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RATTONAL RECREATIONS,

In which the PRINCIPLES of

NUMBERS

AND

NATURAL PHILOSOPHY

Are clearly and copiously elucidated,

BY A SERIES OF

EASY, ENTERTAINING, INTERESTING
EXPERIMENTS.

Among which are

All those commonly performed with the CARDS.

By W. HOOPER, M.D.

VOL. I.

THE THIRD EDITION, CORRECTED.

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ISTORICAL MELICAL (/BRAR)

RATIONAL

RECREATIONS.

VOLUME THE FIRST.

CONTAINING

ARITHMETICAL AND MECHANICAL EXPERIMENTS.



ADVERTISEMENT.

AS the design of this work is to render useful knowledge easy and entertaining, the author has selected the principal part of the experiments from the writers on recreative Philosophy of the last and present centuries: from Baptista Porta to Ozanam and Guyot; the last, especially, has furnished a large number of recreations that are new and pleasing, and from him also are copied several figures that the authors of the experiments they explain have only described. The writers on electricity have also contributed a considerable quantity of recreations, and fuch as for pleafure and furprize are inferior to none. Though this work is, in general, a compilation, some original experiments will be here found, and the whole, perhaps, will appear to be delivered with more perspicuity and concision, and digested. a

gested in a manner more regular than has been hitherto attempted. The principles of each science are, moreover, here laid down in a few plain aphorisms, such as require no previous knowledge, and very little capacity or attention to comprehend; so that the reader will readily discover, at the same time that he admires the phænomena, the source from whence they proceed, and learn, that far from being marvellous or incomprehensible, they are the regular and necessary effects of the laws of nature.

INTRO-

INTRODUCTION.

A MONG the various productions of the prefs, those that are intended for instructive entertainment seem to deserve some degree of attention, and that as well from the difficulty as the utility of the enterprize; for though to offer useful knowledge be sufficiently easy, yet to render that knowledge engaging is oftentimes extremely difficult. Man, careless, froward, stubborn, vain, impetuous, disdains the imputation of

ignorance, and loaths the authoritative dictates of affuming superiority.

Should we not, therefore, endeavour to render useful learning, not dull, tedious, and difguftful, not rugged and perplexing, not auftere and imperious, but facile, bland, delightful, alluring, captivating? that Philosophy, with his fober garb and folemn aspect, when led by the hand of the fportive nymph Imagination, decked in all the glowing ever-varying colours of the skies, may gain admittance to the parties of the gay and and careless; and while his aweful eye restrains the exuberance of her fallies, the beams that dart from her radiant front may play upon his countenance, and diffipate the cloud that

that too frequently hangs over his

Thus will the mind of man be pleafingly enlarged and fortified; he will unavoidably acquire a knowledge of his own ignorance; and by finding the fallacy of what he thought most certain, the evidence of the senses, he will learn to determine with caution on the seeming convictions of the mind, and divest himself of those prepossessions, from whence so many of the evils of life proceed.

Thus may he advance with tranquil fteps through the flowery path of investigation, till arriving at some noble eminence, he beholds, with awful aftonishment, the immense riches in the

bound-

boundless regions of science, and becomes animated to attain a still more lofty station; while his heart is incessfantly rapt with joys of which the grovelling herd have no conception, compared with whose ignorance, the insensibility of the blind and deaf, to the most brilliant harmony of colours, or enchanting melody of sounds, are but trisling impersections.

Though this work is principally intended for the rifing generation, yet they whom a criminal indulgence of their guardians, or a flavish submiffion to their own tyrannic passions, have plunged into sensuality, till incessant fruition hath produced an unconquerable loathing, or till age hath deprived them of appetite, and nought remains of life

life but a wretched hankering after enjoyments they can never more obtain; even they will here find an entrance to new pleafures; they will fee, with grateful admiration, that all bounteous Providence has still in store for them, joys poignant yet tranquil, perpetually increasing, yet never cloying, and that it depends on themselves still to purfue, even to the utmost verge of life, a continual round of variegated pleafures.

To each volume is prefixed, a short description of the plates contained therein, with a reference to the page where they may be found; and to the figures in each plate, is annexed the page where fuch figure is fully described in the work,

At

viii INTRODUCTION.

At the end of each volume is added a table of contents, in which is given a regular abstract of every article; fo that the reader, after having once perused the whole, by looking over the contents, will readily remember how every recreation is to be performed.

DESCRIP-

DESCRIPTION of the PLATES.

PLATE I. p. 20.

Fig. 1. Neper's rods. There are eleven of these rods placed perpendicular and close to each other: on the first is wrote the nine digits, and on the last nine cyphers: the other nine contain a multiplication table.

Fig. 2. Example of the manner of placing the rods for multiplying and dividing.

Fig. 3. The Chinese swan pan. The perpendicular lines within the square ABCD represent bars, that divide it into seven divisions. The five horizontal lines in the upper divisions, and the seven horizontal lines in the lower divisions, on which are small black circles, represent wires;

wires; the circles are balls moveable on those wires, and by bringing them up to the middle bar they express the sum required.

P L A T E II. p. 148.

The mystical dial. The inner circle ILMN turns round on its center O, within the other circle EFGH, so that any letter of the former may be placed against the first letter of the latter, as shall be agreed on. The letters of the one are then wrote for those of the other, as in the example under the figure.

P L A T E III. p. 152.

The mufical cypher. The inner circle ILMN, on which the notes are wrote, turns round within the other circle, as in the last Plate, and the notes are here wrote for the letters, as in the example under the figure.

PLATE IV. p. 166.

- Fig. 1. The machine for visual correspondence ABCD, Fig. 1, is a circle of wood which turns on the centre G: a, b, c, d, are pins by which it turns round. Through its circumference are cut the letters of the alphabet, and between A and Z is an open space.
- Fig. 2, is the pole to which the circle just mentioned is placed by its centre, near P. The board E F, at top, prevents any letter from being seen, except that directly opposite the space in its middle.
- Fig. 3, is the machine for auricular correspondence. The strings to the two bells A and B, which are moveable on the cross-piece C D, are pulled one or more times, according to the letter that answers to the number of founds.

PLATE V. p. 178.

This plate contains the primary mechanic inftruments, or mechanic powers.

Fig.

Fig. 1, 2, 3, 4, are levers of different kinds; each of the other figures have their names annexed to them.

P L A T E VI. p. 186.

Fig. 1 and 2. A dial to go without wheels, fpring, or weight. C D, Fig. 1, is the cylinder, the ends of whose axis, as they descend, point to the hours marked on the columns E F.

Fig. 2, represents the internal structure of the cylinder, which consists of five divisions, in three of which there is water, expressed by the shade.

Fig. 3 and 4. A dial to show the hour by descending an inclined plane. A B, Fig. 3, the external appearance of the dial: g, a hemisphere, on which a figure sits that points to the hour.

Fig. 4, the internal structure of the dial.

P L A T E VII. p. 194.

Fig. 1 and 2, the inferutable lock. AB, Fig. 1, the feutcheon to the lock; C the pinion by which it is fixed in any position.

ABCD,

ABCD, Fig. 2, the twelve wards of the key, which turn round the pipe and are fixed together by the screw E.

Fig. 3, the hand-mill to grind corn, &c. inceffantly, without any animal force. ABCD a fmoke-jack, that turns the rope EF, by which the mill is kept in continual motion.

PLATE VIII. p. 196.

Fig. 1. a carriage to go without any external force. ABCD, the figure of the carriage, with the person who rides in it, and the footman who drives it.

Fig. 2, reprefents the machinery by which it is moved, and which is concealed in a box behind the carriage. C D are two treddles that are pushed down alternately by the man behind the carriage, and by means of the ropes C A, D A, turn the wheels H, H, which being fixed on the same axis with the great wheels I, I, turn them also.

PLATE

P L A T E IX. p. 200.

Fig. 1. The catapulta. ABCD, the frame in which the arrows are placed; E F the fpring by which they are forced out. G the post to which the rope that bends the spring is fastened.

Fig. 2. The failing chariot; AB the body of the chariot; CD the fails; E the rudder, guided by the man at the helm A.

PLATE X. p. 206.

Fig. 1. A carriage to fail against the wind. ABCD the body of the carriage; M the mast: GEFH the fails; K the cogwheel, that takes the teeth placed perpendicular to the sides of the fore-wheels; R the rudder by which it is guided.

Fig. 2. The uninvertible carriage. A B the body of the carriage; C the weight by which it is kept always upright; FGDE are iron circles in which it moves; P the door; O the window, and Q R the fhafts.

PLATE XI. p. 212.

Fig. 1. The case of the columnar dial. AC the capital, that contains the striking part of this dial; GH is the shaft on which are marked the hours; H the index, that by its descent shows the hour. The hand in the circle on the base B, points to the minute.

Fig. 2, shows the machinery of this dial. A is the wheel that moves the minute hand, and which is turned by the weight B, to which is fixed the hour hand H. F and G are two brass wheels fixed on the axis DE. The wheel F raises the end M of the lever MNO, and makes the other end, to which the hammer P is fixed, to strike the bell Q.

PLATE XII. p. 222.

Fig. 1, is an air chronometer. AB is a glass tube; CD the frame in which it is placed; E a piston to let out the air; F the string by which the piston is drawn up; G the handle that confines the string of the piston.

Fig.

- Fig. 2. Shows the form of the piston in the tube.
- Fig. 3. A conical roller to receive the ftring to the index of a dial, when placed over the tube.
- Fig. 2. A lamp chronometer. A is a finall glass lamp, placed in the stand B, C the handle that fupports the style H, and frame DEFG, which is covered with oiled paper, and on which are wrote the figures for the hours.
- Fig. 5. A nocturnal dial. A and B are two wheels of the fame dimension, and concentral; C a pinion: D and E two wheels placed on the fame axis; Fa lamp fixed on the edge of the wheel B; G the weight that gives motion to the whole machine.
- Fig. 6. Is a hollow cone, by which the flame of the lamp F is confined to a particular part of the wheel A.

RATIONAL RECREATIONS.

ARITHMETIC.

DEFINITIONS.

mary principles of numbers, as our readers are supposed to understand the four first rules of arithmetic, addition, subtraction, multiplication, and division; we shall therefore begin with arithmetic powers.

meant the feveral times that number is multiplied into itself. Thus, if 4 be multiplied into itself, the product 16 will be its second power, or square; and if that sum be multiplied by four, the product 64 is the third power, or cube of 4, &c.

Vol. I. B 2 The

- 2. The root of any power is that number from whence it first sprung, or was multiplied: so the square root of 16 is 4; and the cube root of 27 is 3.
- 3. When two numbers are compared together, the first is called the antecedent, and the second the consequent; and the proportion these numbers bear to each other is called their ratio. Thus, the ratio of 27 to 9, is that of 3 to 1.
- 4. When three numbers are compared together, if the difference between each of them be equal, as 2, 4, 6, or, 9, 6, 3, they re faid to be in arithmetic proportion.
 - 5. If three numbers be compared together, and they have one common ratio, that is, the same multiplier or divisor, as 3, 9, 27, or 64, 16, 4, they are in geometric proportion.
 - 6. Whenever the confequent is double the antecedent, they are faid to be in duplicate proportion; but if the antecedent be double the confequent, they are in fubduplicate proportion.

- 7. When any feries of numbers continually increases or decreases by an equal addition or subtraction, as 2, 4, 6, 8, &c. or 18, 15, 12, 9, &c. they are said to be in arithmetic progression.
- 8. When a feries of numbers continually increases or decreases by one common multiplier or divisor, that is, by one common ratio, as 4, 8, 16, 32, &c. or 81, 27, 9, 3, they are in geometric progression.
- 9. If over a feries of numbers in geometric progression, there be placed another in arithmetic progression, whose common difference is 1, as thus 1, 2, 3, 2, 4, 8,
- 4, 5, 32, &c. the latter are called the indices or exponents of the former: and if the geometric feries begin with 1, the other must begin with a cypher, thus, 0, 1, 2, 3, 4, &c.
- 10. The feveral different ways that one number of quantities can be taken out of another greater number, of the same sort,

are called the combinations of the former in the latter. Thus the different ways, that three balls can be taken out of fix, are the combinations of 3 in 6.

any number of quantities can be taken or disposed, are called the permutations of that number; so all the different ways that fix counters can be placed in a line, are the permutations of the number 6.

APHORISMS.

- 1. If two even numbers be added together, or subtracted from each other, their fum or difference will be an even number.
- 2. If two uneven numbers be added or fubtracted, their fum or difference will be an even number.
- 3. The fum or difference of an even and uneven number will be an uneven number.
- 4, The product of two even numbers will be an even number; and the product of two uneven numbers will be an uneven number.

- 5. The product of an even and uneven number will be an even number.
- 6. If two different numbers be divisible by any one number, their sum and their difference will be also divisible by that number.
- 7. If feveral different numbers, divisible by three, be added or multiplied together, their sum and their product will also be divisable by 3.
- 8. If two numbers, divisible by 9, be added together, the sum of the figures in the amount will be either 9, or a number divisible by 9.
- g. If any number be multiplied by g, or by another number divisible by g, the amount of the figures of the product will be either nine, or a number divisable by g.
- 10. In every arithmetic progression, if double the sum of all the terms in any series be divided by the first and last term added together, the quotient will

be the number of all the terms in that feries*.

11. In

- * This and the following aphorisms, relating to progressions, may be applied to many useful purposes besides those mentioned in the course of this work. For example.
- of which he proposes to ride the first day, and to increase the number, by an equal addition, every day to the last, when he intends to ride 100 miles. How long will he be going his journey?

You have here the first term 40, the last term 100, and the sum of all the terms 1120, to find the number of terms: therefore, by aphorism 10, if the double of 1120, that is 2240, be divided by 40 added to 100, the quotient, which is 16, will be the number of terms, or days he will be going.

But, by the 11th aphorism, if the difference between the first and last term, that is 60, be divided by the number of terms less 1, which is 15, the quotient 4 will be the common difference, or number of miles he must add each day.

2. A father intends to lay up 101 toward his daughter's portion the day she is a year old, and to increase the sum as much every year as shall make her fortune, at the end of 20 years, 10001. What will he have to lay up the last year?

Here the first term, number of terms, and sum of the series are given, to find the last term; there11. In every fuch feries, if the difference between the first and last term be divided by

fore by aphorism 12, if from double the sum of the series, which is 2000, you subtract the product of the first term, multiply by the number of terms, that is 200, and divide the remainder, which will be 1800, by the number of terms, the quotient 90 is the last term, or number of pounds he must lay up the last year.

3. A gentleman proposes to plant a number of trees in his grounds, for 20 years together, in regular progression, 20 the first year, and 100 the last. How many trees will he plant?

By aphorism 13, if you multiply the first and last term by the number of terms, and divide the sum of the two products, which is 2400, by 2, the quotient 1200 is the number of trees he must plant.

4. A landlord asks 51. a year for an acre of land, which the farmer thinking too much, the landlord offers to let him a lease of it, for 21 years, at 1d. the first year, 2d. the second year, 4d. the third, and so on, doubling the sum every year. What would the farmer pay the last year? and what would be the average rent for the whole term?

Here the 20th term (which is to be confidered as the last, the first term being one, which neither multiplies nor divides) will be found by the 14th aphorism to be 1,048,576 pence, or 4369l. 15. 4d.

by the number of terms, less 1, the quotient will be the common difference between each term of that series.

- 12. If the product of the number of terms multiplied by the first term, be subtracted from double the sum of the series, and the remainder be divided by the number of terms, the quotient will be the last term.
- 13. If the first and last term be each multiplied by the number of terms, and the sum of the two products be divided by two, the quotient will be the sum of the series.
- 14. In every geometric progression, if any two terms be multiplied together

which is the rent he will pay the last year. But, by aphorism 15, to find the sum of the series, the last term must be multiplied by the ratio 2, which will make it 2,097,152, and from that sum, the first term 1, must be deducted, when it will be 2,097,151, and that sum is to be divided by the ratio 2 less 1, that is by 1; therefore it will remain the same, and confequently be the sum of the series. Then dividing 2,097,151 by 21, the number of years, the quotient 99,864, or 4161. 2s. will be the average rent for each year.

their

their product will be equal to that term which answers to the sum of their two indices. Thus, in the series 1, 2, 3, 4, 5, 2, 4, 8, 16, 32, if the third and fourth terms, 8 and 16, be multiplied together, the product 128 will be the seventh term of that series. In like manner, if the fifth term be multiplied into itself, the product will be the tenth term; and if that sum be multiplied into itself the product will be the twentieth term, &c. Therefore, to find the last, or any other term of a geometric series, it is not necessary to continue the series beyond a few of the first terms.

- 15. In any geometric feries, if you multiply the last term by the common ratio, from the product subtract the first term, and divide the remainder by the ratio, less 1, the quotient will be the sum of that series.
- 16. In all combinations, if from an arithmetic decreasing feries, whose first term is the number out of which the combinations

binations are to be formed, and whose common difference is 1, there be taken as many terms as there are quantities to be combined; and those terms be multiplied into each other: and if from the feries, 1, 2, 3, 4, &c. there be taken the same number of terms, and they be multiplied into each other, and the first product be divided by the fecond, the quotient will be the number of combinations required. Therefore, if you would know how many ways four quantities can be combined in feven, multiply the first four terms of the feries, 7, 6, 5, 4, &c. together, and divide the product, which will be 840, by the product of the first four terms of the series, 1, 2, 3, 4, &c. which is 24, and the quotient 35 will be the combinations of 4 in 7.

17. In all permutations, if the feries 1, 2, 3, 4, &c. be continued to as many terms as there are quantities to be changed, and those terms be multiplied into each other, the product will be the number of permutations fought. Thus, if you would

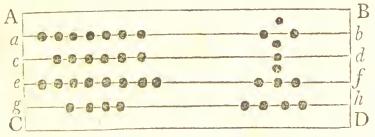
know

know how many permutations can be formed with five quantities, multiply the terms, 1, 2, 3, 4, 5, together, and the product 120 will be the number of all the permutations*.

Previous to the numerical Recreations, we shall here describe certain mechanical methods of performing arithmetical operations, such as are not only in themselves entertaining, but will be found useful on several occasions.

The ROMAN ABACUS.

N a board about a foot long, and of the form of ABCD in the following figure, draw feveral lines, as ab, cd, ef, gh, &c. the number of these lines may be increased at pleasure.



^{*} For farther examples of combinations and permutations, see Recreations XVIII. XIX. &c.

On each of these lines, and on the spaces between them, there are to be placed a certain number of counters, according to the fum or quantity that is to be fet down The counters on the lowest line stand for units, those on the second line for tens. those on the third for hundreds, &c. and the counters between the lines stand always for half the value of those on the line next above. Therefore if you would fet down 7684, you place four counters on the lowest line, eight on the next above, fix on the next, and feven on the uppermost line. Or you may fet down the fame fum by placing part of it on the lines, and the rest between them, as you fee in the figure.

To add or fubtract by this instrument is very easy, as nothing more is necessary than to set on, or take off, a certain number of counters; or place those already on, higher or lower, according to the sum that is to be expressed.

Ву

By this invention a person who has not learned to write may set down any sum of money, or other quantity whatever; for the counters on the several lines, instead of tens, hundreds, &c. may stand for hundred weights, quarters, pounds; or for years, months, days, hours, &c. and, according to the length of the board, several sums of different denominations may be set down at the same time.

NEPER'S RODS.

or pasteboard, as A B C D, (Pl. I. Fig. 1.) into ninety-nine equal parts, as in the figure: in the nine parts next the left hand write the nine digits: in those next the right hand write nine cyphers, and in those at top the nine digits. Separate the remaining divisions into two parts, by a line drawn from the upper angle on the right side, to the lower angle on the left, and on these divisions write

the multiplication table, observing when there are two figures, to place the units in the right hand division, and the tens in the left. Then separate the eleven columns by cutting them as funder from top to bottom, and you will have Neper's rods or bones*.

These rods are to be placed in a box of the length and depth of the square ABCD, and wide enough to hold fix, nine, or as many more of each fort as you please. The uppermost figure of each rod must stand out, above the box, that it may be easily distinguished. The rods have sometimes sigures on each of their four sides to answer different purposes. On the front of the box there must be a ledge to support the rods as they are taken out and placed in order.

To multiply any fum by these rods, suppose 5487 by 273, first, take out the

index

^{*} So called from the inventor J. Neper, baron of Merchifton in Scotland.

index rod of digits next the left hand, and place it against the ledge; then take each of those rods that have at top one of the figures of the multiplicand, beginning with the figure 5, and place them in order as you will fee in Pl. I. Fig. 2. You are then to fet down the fum that stands against each figure of the multiplier, with this caution, that when there are two figures in any fquare, you are to add that in the left division to the figure in the right division of the following fquare, beginning with the right hand column. For example, in the column that stands against 3 in the digits (Fig. 2.) you first set down the 8, and carrying the 1 to the 4 in the next division, you set down 5; then adding the 2 on the second divifion to the 2 in the third, you fet down 4; then adding 1 to 5, you fet down 6, and laftly the figure 1. This may be done almost as fast as you can copy the figures; and fo of the other figures in the multiplier, and the operation will stand as follows:

To divide by thefe rods, suppose 748524 by 2793, place the rods that contain the feveral figures of the divisor, with the index rod, in the fame manner as in the last example, and you will have the product of that divisor by each of the nine digits. Then take the first four figures of the dividend 7485, and look for that number on the rods which is the next less to it; which you will find to be 5586, that stands against the figure 2; you therefore put 2 for the quotient, and fubtracting the last number from the first; bring down another figure from the dividend. You then look again for the nearest fum to that, and fo on till you have taken down all the figures of the dividend, when

when you will find the whole quotient to be 268.

The CHINESE SWAN PAN.

N the fquare frame of wood, ABCD, (Pl. I. Fig. 3.) make four divisions by the bars, EF and GH; and separate three of these divisions into two parts by the lesser bars, ab. In each of the smaller divisions place wires, to be taken out at pleasure; and on each of the wires in the less-hand divisions, string a small ivory ball, or large bead; and on the wires on the right hand division, place four such balls, or beads.

The balls in the left hand divisions, when brought up to the middle bar, stand each for five; and those in the right divisions, when brought to the bar, stand for units.

The balls in the two lower divisions represent integers, or the whole of any Vol., I.

C quan-

RECREATION I.

Any number being named, by adding a figure to that number to make it divisible by nine.

The number named be, for example, 72,857, you tell him who names it to place the number 7 between any two figures of that fum, and it will be divifible by 9. For by aphorism 9, if any number be multiplied by 9, the sum of the figures of the product will be either 9, or a number divisible by 9. But the sum of the figures named is 29, therefore 7 must be added to it to make it divisible by 9.

You may diversify this recreation, by specifying, before the sum is named, the particular place where the sigure shall be inserted, to make the number divisible by 9.

RECREATION II.

A person having an even number of counters in one hand, and an odd number in the other, to tell in which hand the odd or even number is.

in his right hand by an odd number, and the number in his left hand by an even number, and tell you if the fum of the products added together be odd or even. If it be even, the even number is in the right hand; but if it be odd, the even number is in the left hand: as is evident from the first five aphorisms.

Example	le.
right hand 18	In the left 7
Multipliers 3	2
***************************************	Philipping and the second
54	14
14	-
-	
Their fum 68	

C 4	2. Num-

By this instrument all the operations of arithmetic may be readily performed: fuppofe, for example, you would multiply the fum fet down in the division of integers, that is 279 by 3. Begin with the lowest line, and fay 3 times 2 is 6, therefore fet that number up; then on the next row, fay 3 times 7 is 21, therefore instead of 7 fet up I on that line, and carry the two tens to the line below, which will make the number there 8. Then at the upper line fay, 3 times 9 is 27, therefore fet 7 on that line, and carry 2 to the next line below, which will make that number 3. So that the balls on the three lines will then express 837.

If you would divide 279 by 3, begin in like manner with the lowest line; but as 3 cannot be taken in 2, you add the next number to it, and say the threes in 27 are 9, therefore set back the 2 on the lowest line, and place 9, instead of 7, on the next line above; then at the uppermost line

PLATE.I. VOL.I. p 20. Fig. 1. p. 13. Fig. 3. p. 17. Fig. 2. p.15. Parts Units Tens Units
Tens
Hundreds
Thousands
Tens Thousands
Hund Thousands
Millions



line fay, the threes in 9 are 3; therefore instead of g place 3 on that line, and confequently the quotient will be 93. When there is a remainder it may be placed with the divisor, as a fraction, in the upper divisions. When there are many figures in the multiplicand and multiplier, the latter may be placed in the two first divisions of parts, and the former and products in the divisions of integers. In like manner, when there are feveral figures in the dividend and divifor, the former may be placed in the division of integers, the latter in the first two divisions of parts, and the figures of the quotient as they rife, in the remaining two divisions.

It is well worth observing, that by means of this instrument a blind man may be taught to add, subtract, multiply, divide, and perform all the other operations of arithmetic, with as much certainty as another person can by figures.

quantity; those on the uppermost wire stand for tens of such integers, the next for hundreds, and so on, as is expressed, in the sigure. The wires in all the divisions, may be increased to any number you think proper.

The balls in the four upper divisions represent parts of integers; those in the two divisions next the left hand stand for tens; and those in the two other divisions, for units of such parts*.

Now if the fum you would fet down be integers, begin with the balls in the two lower divisions; for example, on the third row from the top bring two balls, of the right hand division, up to the middle bar (fee the Figure); then bring up two on the next row, and one on the same row in the left division; next four on the

top

^{*} This is not the original Swan Pan mentioned by Du Halde, in his History of China, but an improvement on that by Mr. G. Smethurst, of Manchester, published in the Gent. Mrg. for 1748.

top row, and one on the other fide of the fame row; then in the first row of units, from the bottom, and in the right hand division, place two balls, on the second row one, and one also on the fame line in the right hand division of tens: lastly, on the third, row of units place three balls. The balls being thus placed, if the integers be pounds sterling, they will express 2791. 2s. 11\frac{3}{4}d. If the integers be hundred weights, the sum will be 279 cwt. 2 qrs. 11lb. 3oz. or if they be years, they will denote 279 years, 2 months, 11 days, 3 hours.

A part of these balls may represent fractions, either vulgar or decimal; the balls in the first two divisions of parts may stand for the numerators, and those in the other two for denominators; or the numbers in either of these divisions may be added to those in the integers, as decimals*.

^{*} There may also be holes made in the bars where the dots are placed, in which pegs may be occasionally put, to shew that those numbers stand for fractions.

2.	Number in the right hand	7	In the	left	18
	Multipliers	3			2
	-				
	(2 I			36
		36			·
	-				
	Their fum	57			
	_				

RECREATION III.

A person making choice of several numbers, another shall name him the number by which the sum of those numbers is divisible.

two parts: in one part put feveral tickets, on each of which is wrote a number divisible by three, as 6, 9, 15, 36, 63, 120, 213, 309, &c. and in the other part put tickets marked with the number 3 only. From the first part draw a handful of tickets, and after shewing them, put them in again; then open the bag, and defire any one to take out as many tickets as he

thinks proper; flut the bag, and when you open it again offer the other part to another perfon, telling him to take out one ticket only: you then pronounce that ticket to contain the number by which the amount of the other numbers is divifible. For each of those numbers being divisible by 3 their sum also, by aphorism 7, must be divisible by the same number.

RECREATION IV.

To find the difference between two numbers, the greatest of which is unknown.

TAKE as many nines as there are figures in the smallest number, and subtract that sum from the number of nines. Let another person add that difference to the largest number, and taking away the first figure of the amount, add it to the last figure, and that sum will be the difference of the two numbers*.

^{*} See the eighth aphorism.

27, their products will terminate with the nine digits in this order, 9, 8, 7, 6, 5, 4, 3,2,1; the numbers being as follows, 219, 438, 657, 876, 1095, 1314, 1533, 1752, 1971; therefore put into one of the divifions of the little bag, mentioned in the third Recreation, feveral tickets marked with the number 73, and in the other part of the bag the numbers 3, 6, 9, 12, 15, 18, 21, 24, and 27.

Then open that part of the bag where are the numbers 73, and defire a perfon to take out one ticket only, then dextrously change the opening, and defire another person to take a ticket from that part, and when you have multiplied their two numbers together, by knowing the last figure of the product you will readily tell them by the foregoing series, what the other figures are.

RECREATION VIII.

The Magical Century.

If the number 11 be multiplied by any one of the nine digits, the two figures of the product will always be fimilar. As follows:

Place a parcel of counters on a table, and propose to any one to add, alternately, a certain number of those counters, till they amount to a hundred, but never to add more than to at one time. You tell him, moreover, that if you stake first he shall never make the even century, but you will. In order to which you must first stake 1, and remembering the order of the above series, 11, 22, 32, &c. you constantly add, to what he stakes, as many a will make one more than the numbers of that series, that is, as will make 12, 23, 34,

17 will necessarily end at 8, which shews that to be the hour he chose.

That the hour at which the counting ends must be that on which he proposed to rise, will be evident on a little restection; for if he had begun at that hour and counted 12, he would necessarily have come to it again; and calling the number 17, by adding 5 to it, only serves to disguise the matter, but can make no fort of difference in the counting.

RECREATION VI.

A person chusing any two, out of several given numbers, and after adding them together, striking out one of the figures from the amount, to tell you what that sigure was.

SUCH numbers must be offered as are divisible by 9; and when any two of them are added together there must be no cypher in the amount: the figures of that amount,

amount, moreover, must make either 9 or 18. Such are the numbers following; 36, 63, 81, 117, 126, 162, 207, 216, 252, 261, 306, 315, 360, and 432.

These numbers must be wrote on cards; and when any two of them are added together, if a figure be struck out of the sum, it will be what would make the other figures either 9 or 18. For example; if a person chose 126 and 252, their sum will be 378, from which if he strikes out the 7, the remaining sigures 3 and 8 will make 11, to which 7 must be added to make 18.

RECREATION VII.

Two persons chusing two numbers, and multiplying them together, by knowing the last figure of the product to tell the other figures.

IF the number 73 be multiplied by the numbers of the following arithmetical progressions, 3,6,9,12,15,18,21,24, and

For example, Matthew, who is 22, tells Henry, who is older, that he can discover the difference of their ages; he therefore privately deducts 22 from 99, and the difference, which is 77, he tells Henry to add to his age, and to take away the first figure from the amount, and add it to the last figure, and that last sum will be the difference of their ages, As thus:

The difference between Matthew's	} 77
To which Henry adding his age	35
The fum is	112
	12
Then by taking away the first fi-	
gure 1 and adding it to the last figure 2, the sum is	13
Which added to Matthew's age	22
Gives the age of Henry, which is	35

RECRE-

RECREATION V.

To tell, by the dial of a watch, at what hour any person intends to rife.

Let T the person set the hand of the dial to any hour he please, and tell you what hour that is, and to the number of that hour you add, in your mind, 12. Then tell him to count privately the number of that amount upon the dial, beginning with the next hour to that on which he proposes to rise, and counting backwards, first reckoning the number of the hour at which he has placed the hand. An example will make this plain.

Suppose the hour at which he intends to rife be 8, and that he has placed the hand at 5. You add 12 to 5, and tell him to count 17 on the dial, first reckoning 5, the hour at which the index stands, and counting backwards from the hour at which he intends to rife, and the number

&c. till you come to 89, after which the other party cannot make the century himfelf, or prevent you from making it.

If the other party has no knowledge of numbers, you may stake any other number sirst, under 10, provided you take care to secure some one of the last terms, as 56, 67, 78, &c.

This Recreation may be performed with other numbers; and in order to fucceed, you must divide the number to be attained, by a number that has one digit more than what you can stake each time, and the remainder will be the number you must first stake. Observe, that to be sure of success, there must be always a remainder. Suppose, for example, the number to be attained is 52, making use of a pack of cards instead of counters, and that you are never to add more than 6; then divide 52 by the next number above 6, that is, by 7, and the remainder, which

is 3, will be the number you must stake first; and whatever the other stakes, you must add as much to it as will make it equal to the number by which you divided, that is, 7. Therefore if his first stake be 1, you must stake 6, &c. so that your second stake will make the heap 10, your third stake will make it 17, and so on, till you come to 45, when as he cannot stake more than 6, you must make the number 52.

In this, as in the former case, if the other person have no knowledge of numbers, you may stake any number first under 7; or you may let him stake first, only taking care to secure either of the numbers 10, 17, 24, 31, &c. after which he cannot make 52, if you constantly add as many to his stake as will make it 7.

RECREATION IX.

The Confederate Counters.

DRESENT to three persons a ring, a feal, and a fnuff-box, of which defire each person to chuse one, privately. The three persons you discriminate in your mind by the letters A, E, I, and by the fame letters you distinguish the ring, the feal, and the box. Provide 24 counters, of which give the first person A, I, the second person E, 2, and the third person I, 3. Put the 18 remaining counters on the table, and let him that has the ring take as many counters more as he already has; him that has the feal take twice as many as he has, and him that has the box four times as many. While they are taking the counters you retire out of fight, and when they have done you return, and casting your eye on the table, take notice how many counters are left.

The remaining counters will be either 1, 2, 3, 5, 6, or 7, which you are to refer to the vowels in the fyllables of the following verse:

If there be but one counter left, the two vowels in the fyllables par fer denote that the first person has the ring, to which you have assigned the letter A; the second person has the seal, to which you have assigned the letter E; and consequently the third person must have the box. In like manner, if there be six counters remaining, the two vowels in the syllables si grand, shew that the first person has the box, denoted by the letter I; the second person has the ring, to which the letter A is assigned; and consequently the third person has the seal: and so of the rest.

It appears by aphorism 16, that the three articles can be taken only six different ways. Now each of these ways necessarily changes the number of counters to be taken by the three persons: from whence it follows, that the counters remaining on the table will also be of six different numbers; the vowels in the syllables of the verse serve only to aid the memory in discovering the manner in which the three articles are taken.

RECREATION X.

A person privately fixing on any number, to tell him that number.

FTER the person has fixed on a number, bid him double it and add 4 to that sum, then multiply the whole by 5; to the product let him add 12, and multiply the amount by 10. From the sum of the whole let him deduct 320, and tell you the remainder, from which, if you

cut off the two last figures, the number that remains will be that he fixed on.

Example.

Let the number chose be Which doubled is 14 And 4 added to it makes 18 Which multiplied by 5, gives 90 To which 12 being added, it is 102 That multiplied by 10, makes 1020 From which deducting 320, the 700 remainder is And by striking off the two cyphers, it becomes the original number

RECREATION XI.

Three dice being thrown on a table, to tell the number of each of them, and the order in which they stand.

ET the person who has thrown the dice double the number of that next his left hand, and add 5 to that sum; then multiply the amount by 5, and to the product add the number of the middle die; then let

D₃ the

the whole be multiplied by 10, and to that product add the number of the third die. From the total let there be fubtracted 250, and the figures of the number that remains will answer to the points of the three dice as they stand on the table.

Example.

Suppose the points of the three	dice
thrown on the table to be 4, 6, and	2.
Then the double of the first die will l	oe 8
To which add — — —	5
	13
	5
That fum multiplied by 5 will be	65
To which add the number of the middle die — —	6
And multiply the fum by	71
Tille multiply the full by	10
To that product add the number?	710
To that product add the number of the third die — —	2
AJ. C	712^
And from the total fubtracting	250
The three remaining figures	462
will answer to the numbers on the c	lice,
and shew the order in which they star	nd.

RECRE-

RECREATION XII.

To tell the number a person has fixed on, without asking him any questions.

THE person having chose any number from 1 to 15, he is to add 21 to that number, and triple the amount. Then

- 1. He is to take the half of that triple, and triple that half.
- 2. To take the half of the last triple, and triple that half.
 - 3. Take the half of the last triple.
 - 4. Take the half of that half.

In this operation it appears there are four cases or stages where the half is to be taken: the three first are denoted by one of the eight following Latin words, each word being composed of three syllables, and those that contain the letter i, refer to those cases* where the half cannot be taken

* These cases being different in all the numbers that can be chose, they are thereby distinguished.

without a fraction; therefore in those cases the person who makes the deduction is to add I to the number to be divided. The fourth case shews which of the two numbers annexed to every word, has been chosen; for if the fourth half can be taken, without adding I, the number chose is in the first column, but if not, it is in the second column.

The words.	The numbers the	ey denote.
Mi-fe-ris	8	0
Ob-tin-git	I	9
Ni-mi-um	2	10
No-ta-ri	3	11
In-fer-nos	4	12
Or-di-nes	13 -	5
Ti-mi-di	6	14
Te-ne-ant	15	7

Example.

Ziverrop vo.			
Suppose the number chose to be			
To which is to be added			
	Simple proper		
	10		
Then the triple of that number is	30		
The half of which is			
The triple of that half must be			
And the half of that*			
The triple of that half			
The half of that*			
And the half of that half*	35 18		

While the person is persorming the operation, you remark, that at the second and third stage he is obliged to add 1. and consequently that the word ob-tingit, in the second and third syllables of which is an i, denotes that the number must be either 1 or 9; and by observing that he cannot take the last half without adding 1, you know that it must be the

^{*} At all the stages thus marked, I must be added in order to take the half without a fraction.

number in the fecond column. If he should make no addition at any one of the four stages, the number he chose must be 15, as that is the only number that has no fraction at either of the divisions.

RECREATION XIII.

Thirty foldiers having deferted, fifteen of whom are to be punished; so to place the whole number in a ring, that you may save any fifteen you please, and it shall seem to be the effect of chance.

THE men must be placed according to the numbers annexed to the vowels in the words of the following verse:

Po-pu-le-am vir-gam ma-ter re-gi-na 4 5 2 1 3 1 1 2 2 3 1 fé-re-bat.

2 2 I

Therefore you place 4 of those you would fave first, then 5 of those you would punish, then 2 of those to be saved, and 1

to be punished; and so on*. You then enter the ring, and beginning with the first of the sour men you intend to save, you tell 9, and the ninth man is turned out to be punished. You go on telling 9 more, and the second 9 will fall on one you intend to punish; and so of the rest.

RECREATION XIV.

Some person in company having put a ring privately on one of his fingers; to name the person, the hand, the finger, and the joint, on which it is placed.

ET a third person double the number of the order in which he stands who has the ring, and add 5 to that number; then multiply that sum by 5, and to the product add 10. Let him next add 1 to last number if the ring be on the right hand, and 2 if on the left, and multiply the whole by 10: to this product he must

^{*} You will observe that each vowel denotes the number that is to be placed, as a 1, e 2, i 3, &c.

add the number of the finger (counting the thumb as the first finger) and multiply the whole again by 10. Let him then add the number of the joint; and, lastly, to the whole join 35.

He is then to tell you the amount of the whole, from which you are to fubtract 3535; and the remainder will confift of four figures, the first of which will express the rank in which the person stands, the second the hand (the number 1 signifying the right hand, and 2 the left), the third number the singer, and the sourth the joint.

Example.

Suppose the person who stands the third in order has put the ring upon the second joint of the thumb of his left hand; then

RECREATIONS.	45				
The double of the rank of the third person is	6				
To which add	_5				
Multiply the fum by	J I 5				
	55				
To which add And the number of the left hand	10				
Which being multiplied by					
To which add the number of the thu	670 mb 1				
And multiply again by	671				
Then add the number of the joint And laftly the number	6710 2 35				
From which deducting	6 ₇₄₇ 3535				
The remainder is	3212				

Of which, as we have faid, the 3 denotes the third person, the 2 the left hand, the 1 the thumb, and the last 2 the second joint.

Of arithmetical magic squares.

Magical fquare of this fort confifts of numbers in arithmetic progression, fo disposed in parallel and equal ranks, that the sum of each row, taken either perpendicularly, horizontally, or diagonally, is equal; as in the second figure.

	Fig. 1. Natural fquare.				Fig. 2.					
					' Magical fquare.					
	A		G		В	A				В
	I	2	3	4	5	ΙΙ	24	7	20	3
E	6	7	8	9	ΙO	4	I 2	25	8	16
	II	I 2	13	I 4	15 F	¹ 7	5	13	2 I	9
	16	17	18	19	20	IO	18	_I	14	22
		22	12			23	6	19	2	15
(3		H		D	C				D

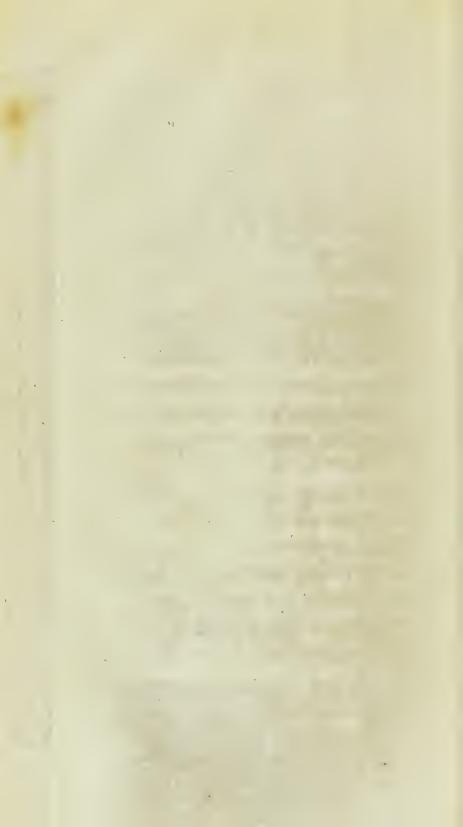
Any five of the fums in this magic fquare taken in a right line, make 65. You will observe that the five numbers in the diagonals AD and BC of the magical fquare, answer to the horizontal and vertical ranks EF and GH in the natural fquare; and that 13 is the central number of both fquares.

To form a magical square, first transpofe the two ranks in the natural fguare. just mentioned, to the diagonals of the magic square; then place the number 1 under the central number 13, and the number 2, in the next diagonal downward. The number 3 should be placed next in the fame diagonal line; but as there is no room in the fquare, you are to place it in that part it would occupy if another fquare were placed under this. For the fame reason the number 4, by following the diagonal direction, falling out of the fquare, it is to be put in the part it would hold in another fquare, placed by the fide of this: you then proceed to the numbers 5 and 6, still descending; but as the place 6 should hold is already filled, you then go back to the next diagonal, and confequently place the number 6 in the fecond case under the number 5, so that there may remain an empty case between the two numbers. The fame method is to be taken whenever you find a cafe already filled.

You proceed in this manner to fill all the empty cases in the angle where the number 15 is placed; and as there is no place for the number 16 in the same diagonal descending, you must place it in the part it would hold in another square, and continue the same method till all the cases are filled. This method will serve equally for all forts of arithmetic progressions composed of odd numbers*; those composed of even numbers being too complicate and abstruse for recreations.

* M. Ozanam, who has wrote very learnedly on magical fquares, observes, that the Egyptians, and the Pythagoreans, their disciples, held them in great veneration. They were dedicated by them, he says, to the seven planets. Saturn had a square of nine cases assigned him; Jupiter, one of 16 cases; Mars, one of 25; Venus, 49; and Mercury, 64 cases: to the Moon they gave a square of 81 cases; and to the Deity, one of a single case, as unity can never be multiplied nor divided, but is for ever unchangeable.

VOL. I. p. 48. PLATE. II. 00 Ma un jvc iumm svar vgrx qu cd jvc dlhmm they h yrkdurk hkt juc ahj dgumm ahlr h dbha vyyvduguvk _



RECREATION XV.

The series of numbers from 1 to 25 being wrote on that number of cards, after you have shuffled them, to deal them to five persons, either by twos or threes, at the option of the parties, and the amount of the numbers on each one's cards to be the same.

IN disposing these cards you must have recourse to the magical square in the last Recreation, and observe to put the two cards that have the numbers 11 and 4 at top; those cards that have 24 and 12 next, and so continue, by 2 and 2, to the last number of that rank, 16, which must be wrote on a card a little wider than the rest. You must follow the same method with the next three numbers 17, 10, 23, and so on to the last three 9, 22, 15, as is fully explained in the following table.

Vol I.

Cards.	Numbers.
I 2	First person.
3	24)
	Second perfon.
4 5 6	${7 \choose 25}$ Third perfon.
× 7. 8	Fourth person.
9 10 wide	$\left\{\begin{array}{cc} 3 \\ \text{card} \end{array}\right\}$ Fifth perfon.
II	17)
12	First person.
13	
14	Second person.
16	6
17	13)
18	Third person.
19	
2 I	Fourth person
22	Fourth person.
23	9)
24	Fifth perfon.
25	15)

The cards being thus difposed, or becoming so by being shuffled in the manner

ner we shall explain farther on, when we treat of the combination of cards, you offer to deal them by twos or threes sirst: if it be required to deal them by twos sirst, there is no occasion to cut them; but if they are to be dealt by threes, they must be cut, that he who cuts them may divide the pack exactly in that part where the wide card is, and that the sisteen cards that were at the bottom may be at top. Observe, you must seel the cards before you deal, in order to know if they be cut at the wide card; if not, they must be cut again, or you may cut them yourself.

It is evident by the foregoing table, which is formed after the magic fquare, that the numbers on each person's cards must necessarily amount to the same number, sixty-sive.

RECREATION XVI.

To deal the 32 cards of the game of piquet to four persons, after you have shuffled them, and the parties have chose whether you shall deal by twos or threes; in such manner, that all the cards in each person's hand shall be of the same suit.

FIRST, dispose the cards in the following order, and observe that the eighth card must be a little larger than the rest.

vari	I little be a little in o
1 2	Ace Seven of Hearts. First person.
3 4	King Spades. Second person.
56	Knave Diamonds. Third person.
78	Ace Knave Clubs. Fourth perfon.
	wide card
9	King Eight Hearts. First person.
12 •3	Ace Knave Spades. Second person.
	15 Ace

15 16	Ace Seven Nine Diamonds. Third person.
17	
18	King Chal Fourth rowfor
20	Ten Nine Clubs. Fourth person.
2 I	Queen Knave Hearts. First person.
,22	Knave Hearts. First person.
23	Ten
24	Queen Nine Seven Spades. Second person.
25	Nine Spades. Second perion.
26	Seven J
27	King Queen Ten Diamonds. Third person.
28	Queen Diamonds. Third person.
29	Ten)
30	Queen)
31	Queen Eight Clubs. Fourth perfon. Seven
32	Seven)

You then follow the same method as in the preceding Recreation: if the cards are required to be dealt by twos first, they are not to be cut, but you deal, once two and twice three. If they are to be dealt by threes first, they must be cut at the place of the wide card, and then dealt by twice three and once two.

Of geometrical magic squares.

THE same method we have given for filling up the cases or divisions of an arithmetic magic square, is to be followed in these. We shall confine ourselves here to examples of the three following geometric squares, containing nine divisions each, which are filled up with three different progressions, applicable to the following Recreation.

Fig. 1.	Fig. 2.	Fig. 3.
16 512 4	24 768 6	56 179 214
8 32 128	12 48 192	28 112 448
256 2 64	384 3 96	896 7 224

You will observe, that in every geometric square, the product of the numbers in each row, whether taken vertically, horizontally, or diagonally, is constantly the same.

RECREATION XVII.

Several different numbers being wrote upon cards, to Shuffle them, and deal the whole, or part of them, to three perfons, in Such manner that each one multiplying the numbers on his cards together, the product of each perfon's cards shall be the same; and to repeat the recreation after having shuffled the cards a second time.

RITE upon feven-and-twenty cards the numbers that are in the foregoing squares, and dispose them in the following order:

I	16	First person.
2	512	Second person.
3	4	Third person.
4	8	Ist person.
5	32	2d person.
5	128	3d person.
7	256	Ist person.
8	2	2d person.
9	wide card 64	3d person.
10	24	Ist person.
II	768	2d person.
12	6	3d person.
	F	4





RECREATION XVIII.

To find the number of changes that may be rung on twelve bells.

Tappears by the 17th aphorism, that nothing is more necessary here, than to multiply the numbers from 1 to 12 continually into each other, in the following manner, and the last product will be the number fought.

RECREATION XIX.

Suppose the letters of the alphabet to be wrote
fo small that no one of them shall take up
more space than the hundredth part of a
square inch: to find how many square
yards it would require to write all the permutations of the 24 letters in that size.

BY following the fame method as in the last recreation, the number of permutations of the 24 letters will be found to be

62,044,840,173,323,943,936,000

Now the inches in a fquare yard being 1296, that number multiplied by 100 gives 129600, which is the number of letters each fquare yard will contain; therefore if we divide 62,044,840,173,323,943,936,000 by 129600, the quotient, which is 478,741,050,720,092,160, will be the number of yards required, to contain the above mentioned number of permutations.

But





cards may be taken out of 52, and confequently the number fought.

The ARITHMETIC TRIANGLE.	A I B	2.1	3. 3. I 4. 6. 4. I	5. 10. 10. 5. 1 6. 15. 20. 15. 6. 1	8. 28. 56. 70. 56. 28. 8. I	9. 36. 84. 126. 126. 84. 36. 9. 1 10. 45. 120. 210. 252. 210. 120. 45. 10. 1	11 11. 55. 165. 330. 462. 462. 330. 165. 55. 11. 1 12 a 12. 66. 220. 495. 792. 924. 792. 495. 220. 66. 12. 1 b
The	1 Rank					I	a 12. 66,
	hed	N	m 4	63	C-00	100	11

The conftruction of this table is very fimple. The line A a confifts of the first twelve numbers. The line A b confifts every where of units; and second term 3,

of the line B c, is composed of the two terms 1 and 2 in the preceding rank: the third term 6, in that line, is formed of the two terms 3 and 3 in the preceding rank: and so of the rest; every term, after the first, being composed of the two next terms in the preceding rank; and by the same method it may be continued to any number of ranks. To find by this table how often any number of things can be combined in another number, under 13, as suppose 5 cards out of 8; in the eighth rank look for the fifth term, which is 56, and that is the number required.

Though we have shewn in the foregoing recreations the manner of finding the combination of all numbers whatever, yet as this table answers the same purpose, for small numbers, by inspection only, it will be sound useful on many occasions; as will appear by the following recreations.

RECREATION XXII.

To find how many different founds may be produced by striking on a harpsichord two or more of the seven natural notes at the same time.

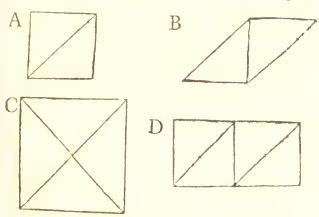
,1 .	THE combinations of two in feven, by the foregoing tri-	2 €
	angle are	
	The combinations of 3 in 7, are	35
	· · · · · · · · · · · · · · · · · · ·	35
4.	The combinations of 5, are	2 I
5.	The combinations of 6, are	7
6.	The feven notes all together once	I
	Therefore the number of all the founds will be	20

RECREATION XXIII.

Take four square pieces of pasteboard, of the same dimension, and divide them diagonally, that is by drawing a line from two opposite angles, as in the figures, into 8 triangles; paint

paint 7 of these triangles with the primitive colours, red, orange, yellow, green, blue, indigo, violet, and let the eighth be white. To find how many chequers or regular four-sided figures, different either in form or colour, may be made out of those eight triangles.

IRST by combining two of these triangles there may be formed either the triangular square A, or the inclined square B, called a rhomb. Secondly, by combining sour of the triangles, the large square C, may be formed; or the long square D, called a parallelogram.



Now the first two squares, consisting of two parts out of 8, they may each of them, Vol. I. F by

by the eighth rank of the triangle be taken 28 different ways, which makes 56. And the last two squares, consisting of sour parts, may each be taken by the same rank of the triangle 70 times, which makes

140
To which add the foregoing number 56 and the number of the different squares that may be formed of the eight triangles, will be

RECREATION XXIV.

A man has 12 different sorts of flowers, and a large number of each sort. He is desirous of setting them in beds or flourishes, in his parterre. Six flowers in some, 7 in others, and 8 in others; so as to have the greatest variety possible; the flowers in no two beds to be the same. To find how many beds he must have.

by the last rank of the triangles, are

2. The combinations of 7 in 12, are 792

3. The combinations of 8 in 12, are 495

Therefore the number of beds

and 2211

RECREATION XXV.

To find the number of chances that may be thrown on two dice.

A S each die has 6 faces, and as every face of one die may be combined with all the faces of the other, it follows, that 6 multiplied by 6, that is 36, will be the number of all the chances: as is also evident from the following table.

Points.	Numb. of Numb. o chances. points.	£
2 1.1 3 2.1 1.2 4 3.2 3.1 1.3 5 4.1 1.4 3.2 2.3 6 3.3 5.1 1.5 4.2 2.4 7 6.1 1.6 5.2 2.5 4.3 3.6 5.4 4.5 9 6.3 3.6 5.4 4.5 10 5.5 6.4 4.6 11 6.5 5.6 12 6.6	3.4 6 42	

It appears by this table, 1. That the number of chances for each point continually encreases to the point of seven,

therefore if two points are proposed to be thrown, the equality, or the advantage of one over the other, is clearly visible*.

The whole number of chances on the dice being 252, if that number be divided by 36, the number of different throws on the dice, the quotient is 7: it follows therefore, that at every throw there is an equal chance of bringing seven points.

As there are 36 chances on the dice, and only 6 of them doublets, it is 5 to 1, at any one throw, against throwing a doublet.

By the same method the number of chances upon any number of dice may be found: for if 36 be multiplied by 6, that

^{*} It is eafy from hence to determine whether a bet proposed at hazard, or any other game with the dice be advantageous or not; if the dice be true: which, by the way, is rarely the case for any long time together, as it is so easy for those that are possessed of a dexterity of hand to change the true dice for salse.

product, which is 216, will be the chances on 3 dice; and if that number be multiplied by 6, the product will be the chances on 4 dice, &c.

RECREATION XXVI.

To discover the number of points on 3 cards, placed under three different parcels of cards.

OU are first to agree that the acc shall tell eleven, the pictured cards ten each, and the others according to their number of points; as at the game of piquet. Then propose to any one to choose 3 cards, and over each of them to put as many cards as will make the number of the points of that card 15. Suppose, for example, he choose a 7, a 10, and an ace: then over the 7 he must place eight cards: over the 10, five cards, and over the ace, four. Take the remainder of the cards, and feeming to look for some card among them, tell how many there are, and F 3

and adding 16 to that number, you will have the number of points on the three cards. As in this inftance, where there will remain 12 cards, if you add 16 to that number it will make 28, which is the number of points on the three cards*.

RECREATION XXVII.

The ten duplicates.

TAKE twenty cards, and after any one has shuffled them, lay them down by pairs on the board, without looking at them. Then defire several persons to look each of them at different pairs, and remember what cards compose them. You then take up all the cards, in the order they lay, and place them again on the table, according to the order of the letters in the following words.

^{*} If this Recreation be performed with a pack of quadrille cards, the number added to the remaining cards must be eight.

M	U	T	U	S
I	2	3	4	5
D	E	D	I	T
6	7	8	9	10
N	O	\mathbf{M}	E	N
ΙI	12	13	14	15
C	0	C	I	S*
16	17	18	19	20

Now you will observe that these words contain ten letters repeated, or ten pair of letters. Therefore you ask each person which row, or rows, the cards he looked at are in; if he say they are in the first row, you know that they must be the second and sourth: if in the second and sourth rows, they must be the ninth and nincteenth, and so of the rest.

^{*} These words convey no meaning. The last word is sometimes wrote Coecis; but that being no Latin word, can make no sense with the others. If, indeed, it was Cœcis, a sort of sense might be made out: but then the æ would by no means answer the o in Nomen, as it must do to perform the Recreation.

RECREATION XXVIII.

To name the number of cards that a person shall take out of the pack.

fo dispose a piquet pack of cards, that you can easily remember the order in which they are placed. Suppose, for example, that they are placed according to the words in the following line;

Seven aces, eight kings, nine queens, and ten knaves.

And that every card be of a different fuit, following each other in this order; fpades, clubs, hearts, and diamonds. Then the eight first cards will be the seven of spades, ace of clubs, eight of hearts, king of diamonds, nine of spades, queen of clubs, ten of hearts, and knave of diamonds; and so of the rest*.

^{*} This Recreation may be farther diversified, by placing the cards in such manner, by the table for thirty-two numbers, that after they have been shuffled once or twice, they may come into the above order.

You show that the cards are placed promiscuously, and then offer them with the backs upward, to any one, that he may draw what quantity he pleafe; which when he has done, you dexterously look at the card that precedes, and that which follows those he has taken. After he has well regarded the cards, you take them from him, and putting them into different parts of the pack, shuffle them, or give them to him to shuffle. During which you recollect, by the foregoing line all the cards he took out; and as you lay them down, one by one, you name cach card.

This is a pleasing Recreation for those that have a good memory; they that have not, should never attempt it.

RECREATION XXIX.

A century of different names being wrote on the cards, to tell the particular name which any person has thought on*.

N ten cards write a hundred different names, observing only, that the last name on each card begin with one of the letters of the word, INDROMACUS, which letters, in the order they stand answer to the numbers 1, 2, 3, &c. to 10. On ten other cards write the same names, with this restriction, that the first name on every card must be taken from the first of the other cards, whose last name begins with I: the second name must be taken from that whose last name begins with N: and so of the rest. Then let any one choose a card out of the first ten, and after he has fixed on a name

^{*} This is called the Impenetrable Secret; though it is one of the most easy Recreations with the cards.

give it you again, when you carefully note the last name, by which you know the number of that card. You then take the other ten cards, and after shuffling them, show them to the person one by one, and ask if he see the name he chose, and when he fays he does, you look to that name which is the fame in number from the top, with the number of the card he took from the other parcel, and that will be the name he fixed on. As for example, suppose he took out the card that had the word Daphnis at the bottom, which is the third card, and that he fixed on the name Galatea, then that word will necessarily be the third on the other card.

Order of the words on the first ten cards.

Order of	the words	on the first to	en caras.
First Card	Second	Third	Fourth
Celadon	Pomona	Deucalion	Licas
Andromeda	Omphalus	Hefiona	Calypso
Silenus	Ariadne	Galatea	Medea
Acis	Lifis	Thetis	Adonis
Eglea	Flora	Atys	Ceres
Sirincus	Danae	Palamedes	Caffandra
Thyrfis	Alcander	Melibæus	Pales
Polyphemus	Tirelias	Orion	Menelaus
Proteus	Isforia	Nifus	Glaucus
Tafon	Narcissus	Daphnis	Rophelina
Fifth	Sixth	Seventh	Eighth
Latona	Icarus	Ganymede	Leander
Hilas	Clitander	Aristea	Peleus
Thisbe	Alcinous	Hyacinthus	Calista
Diana	Endimion	Circe	Cadmus
Palæmon	Alcidon	Mopfa	Pfyche
Hebe	Iphis	Piramus	Semele
Sappho	Achelous	Philemon	Iphigenia
Acteon	Philomela	Astrea	Silvia
Medufa	Cephalus	Pelias	Alpheus
Orpheus	Mirtilus	Adrianus	Coridon
Ni	nth	\mathcal{I}	enth
Hipolitus	Efon	Dryope	Hander
Corilas	Califfus	Nelfus	Isidora
Procris	Arachne	Philoctetes	Melicerte
Capariffa	Pirus	Marfias	Riblis
Arethufus	Vertumn	us Licas	Silvander

Order

Order of the words on the last ten cards.

Oraer o	ine words	on the light	ch cultus.
First Card	Second	Third	Fourth
Celadon	Andromeda	Silenus	Acis .
Pomona	Omphalus	Ariadne	Lisis
Deucalion	Hesiona	Galatea	Thetis
Licas	Calyplo	Medea	Adonis
Latona	Hilas	Thifbe	Diana
Icarus	Clitander	Alcinous	Endimion .
Ganymede	Aristea	Hiacinthus	Circe
Leander	Peleus	Calista	Cadmus
Hypolitus	Corilas	Procris	Caparissa
Dryope	Neffus	Philo&tetes	Marsias
Fifth	Sixth	Seventh	Eighth
Eglea	Sirineus	Thyrsis	Polyphemus
Flora	Danae	Alcander	Tirefias
Atys	Palamedes	Melibæus	Orian
Ceres	Cassandra	Pales	Menelaus
Palæmon	Hebe	Sappho	Acteon
Alcidon	Iphis	Archelous	Philomela
Mopfa	Piramus	Philemon	Astrea
Pfyche	Semele	I phigenia	Silvia
Arethufus	Efon	Calistus	Arachne
Licas	Isander	Ifidora	Melicerte
N	inth	\mathcal{I}	enth
Proteus	Cephalus	Jafon	Myrtilus
Isforia	Pelias	Narcissus	Adrianus
Nifus	Alpheus	Daphnis	Corydon
Glaucus	Pirus	Rophelina	Vertumnus
Medula	Riblis	Orpheus	Silvander

Instead

Instead of ten cards, there may be twenty to each parcel, by adding duplicates to each card, which will make the Recreation appear the more mysterious, and will not at all embarrass it, as you have nothing to remember but the last name on each card. Or instead of names, you may write questions on one of the parcels, and answers on the other.

Of the combinations of the cards.

of many recreations, as well on numbers, letters, and other fubjects, as on the cards; and the effect here produced by them is the more furprising, as that which should feem to prevent any collusion, that is, the shuffling of the cards, is, on the contrary, the cause from whence it proceeds.

It is a matter of indifference what numbers are made use of in forming these tables. We shall here confine ourselves to such as are applicable to the subsequent Recre-

Recreations. Any one may construct them in fuch manner as is agreeable to the purposes he intends they shall answer.

To make them, for example, correspond to the nine digits and a cypher, there must be ten cards, and at the top of nine of them must be wrote one of the digits, and on the tenth a cypher. These cards must be placed upon each other in the regular order, the number I being on the first, and the cypher at bottom. You then take the cards in your left hand, as is commonly done in shuffling, and taking off the two top cards, 1 and 2, you place the two following, 3 and 4, upon them; and under those four cards the three following 5, 6, and 7: at the top you put the cards 8 and 9, and at the bottom the card marked o. Constantly placing in fuccession 2 at top and 3 at bottom, and they will then be in the following order:

8.9..3.4..1.2...5.6.7..0

If you shuffle them a second time, in the same manner, they will then stand in this order:

Thus, at every new shuffle, they will have a different order, as is expressed in the following lines:

1	shuffle	8.9.3.4.1.2.5.6.7.0
2		6.7.3.4.8.9.1.2.5.0
3		2.5.3.4.6.7.8.9.1.0
1		9.1.3.4.2.5.6.7.8.0
5		7.8.3.4.9.1.2.5.6.0
6		5.6.3.4.7.8.9.1.2.0
7		1.2.3.4.5.6.7.8.9.0

It is a remarkable property of this number, that the cards return to the order in which they were first placed, after a number of shuffles, which added to the number of columns that never change the order, is equal to the number of cards. Thus the number of shuffles is 7, and the number of columns in which the cards marked 3, 4, &c. never change their places is 3, which are equal to 10, the number of the cards.

cards. This property is not common to all numbers; the cards fometimes returning to the first order in less number, and fometimes in a greater number of shuffles than that of the cards.

Though the cards are here directed to be shuffled by twos or threes only, yet tables may be constructed with equal facility for shuffling them by 2 and 1, 3 and 4, or any other number whatever; observing that the fewer cards are taken together the less liable you will be to err.

Note, Before you venture to perform these Recreations, you should accustom yourfelf to shuffle the cards exactly and readily; which will be eafily attained by practice.

TABLES OF COMBINATIONS,

Constructed on the foregoing principles.

TABLE I.*

FOR TEN NUMBERS.

Order before shuffl	ing. After 1st flius	Ae. After the 2d.	After the 3d.
I	8	6	2
2	9	7	5
3	3	3	3
4	4	4	4
5	I	8	6
5	2	9	7
7	5	I	8
8	6	2	9
9	7	5	I
0	0	O	O

^{*} These tables and the following Recreations at piquet, except the 36th, appear to have been composed by Mr. Guyot.

TABLE II.

FOR TWENTY FOUR NUMBERS.

Order before shuffling.	After 1st shuffle.	After the 2d	After the 3d.
I	23	21	17
2	24	22	20
3	18	I 2	2
4	19	15	7
5 6	13	5	13
6	14	5 6	14
7	8	9	
8	9	9	18
9	3	18	12
10	4	19	15
1.1	I	23	21
12	2	24	22
13	5 6	13	5
14		14 8	5 6
15	7	8	9
16 .	10	4	19
17 18	11	1	23
	12	2	24
19	15	7	8
20 2 I	16	10	4
	17	II	I
22	20	16	10
23 24	21	17	11
	22	20	16

TABLE III.

FOR TWENTY SEVEN NUMBERS.

Order before shuffling	g. After ist shuffle.	After the 2d.	After the 3d.
I	23	21	17
, 2	24	22	20
	18	12	2
3 4 5 6	19	15	7
4			13
5	13	5 6	14
	14		
7	8	9	3 18
8	9	3	
9	3	18	12
10	4	19	16
II	I	23	2 I
12	2	24	22
13	5	13	5
14	5 6	14	5 6 9
15	7	8	9
16	10	4.	19
	11	î	23
17 18	12	2	24
19	15	7	8
20	16	10	4
21	17	ΙΙ	I
	20	16	10
22	21	17	II
23	22	20	16
24		25	25
25	25 26	26	26
26		27	27
27	27	1	- /

TABLE IV.

FOR THIRTY TWO NUMBERS.

	FOR THI	IRIXI	WO NOME	EKJ.
ider l	before shuffling.	After the tst s	huffle. After the 2d.	After the 3d.
	I	28	26	22
	2	29	27	25
	3	23	17	7
	4	24	20	12
	5 6	18	10	9
	6	19	II	3
	7	13	I	28
	8	14	2	29
	9	8	14	2
	10	9	8	14
	II	3	23	17
	12	4	24	20
	13	I	28	26
	14	2	29	27
	15	5 6	18	10
	16		19	11
	17	7	13	1
	18	10	9	8
	19	11	3	23 24
	20	12	4	18
	21	15	9 3 4 5 6	19
	22 23	16 17	7	13
		-	12	4
	24 25	20 2 I	15	
	26	22	16	5
		25	21	15
	² 7 ₂ 8	26	22	16
	29	27	25	21
	30	30	30	30
	31	31	31	31
	32	32	32	32

RE-

RECREATION XXX.

Several letters that contain no meaning, being wrote upon cards, to make them, after they have been twice shuffled, give an answer to a question that shall be proposed; as for example, What is Love?

ET 24 letters be wrote on as many cards, which, after they have been tice fhuffled, shall give the following anfwer:

A dream of joy that soon is over.

First, write one of the letters in that line on each of the cards. Then write the answer on a paper, and assign one of the 24 first numbers to each card, in the following order:

A DREAM OF JOY THAT

1 23456 78 9 10 11 12 13 14 15

S O O N I S O'ER.

16 17 18 19 2021 22 23 24

† These letters should be wrote in capitals on one of the corners of each card, that the words may be cassly legible when the cards are spread open: Next, write on another paper a line of numbers, from 1 to 24, and looking in the table for 24 combinations you will fee that the first number after the second shuffle is 21, therefore the card that has the first letter of the answer, which is A, must be placed against that number in the line of numbers you have just made * in like manner the number 22 being the second of the same column, indicates that the card which answers to the second letter, D, of the answer, must be placed against that number: and so of the rest. The cards will then stand in the sollowing order:

OOFSAMNTO I S R H A E O'E

18 19 20 21 22 23 24 J O R A D Y T

From whence it follows that after these cards have been twice shuffled they must

^{*} For the same reason if you would have the anfwer after one shuffle, the cards must be placed according to the first column of the table: or if after three shuffles, according to the third column.

infallibly stand in the order of the letters in the answer.

Observe 1. You should have several questions with their answers, consisting of 24 letters, wrote on cards: these cards should be put in cases, and numbered, that you may know to which question each answer belongs. You then present the questions; and when any one of them is chose, you pull out the case that contains the answer, and shewing that the letters wrote on them make no sense, you then shuffle them, and the answer becomes obvious.

2. To make this Recreation the more extraordinary, you may have three cards on each of which an answer is wrote; one of which cards must be a little wider, and another a little longer, than the others. You give these three cards to any one, and when he has privately chose one of them he gives you the other two, which you put into your pocket without looking at

them,

them, having discovered by feeling which he has chose. You then pull out the case that contains the cards that answer to his question, and perform as before.

3. You may also contrive to have a long card at the botton, after the second shuffle. The cards may be then cut several times, till you perceive by the touch that the long card is at bottom, and then give the answer; for the repeated cuttings, however often, will make no alteration in the order of the cards.

The fecond of thefe observations is applicable to some of the subsequent Recreations, and the third may be practised in almost all experiments with the cards. You should take care to put up the cards as soon as the answer has been shewn: so that if any one should defire the Recreation to be repeated, you may offer another question, and pull out those cards that contain the answer.

Though this Recreation cannot fail of exciting at all times pleafure and furprize, yet it must be owned that a great part of the applause it receives arises from the address with which it is performed.

RECREATION XXXI.

The twenty-four letters of the alphabet being wrote upon so many cards, to shuffle
them, and pronounce the letters shall then
be in their natural order; but that not
succeeding, to shuffle them a second time,
and then shew them in proper order.

RITE the 24 letters on the cards in the following order:

1 2 3 4 5 6 7 8 9 10 11 12 R SH Q EFT P G U X C 13 14 15 16 17 18 19 20 21 22 23 24 N O D Y Z I K & A B L M

The cards being disposed in this manner, shew them upon the table, that it may appear they are promiscuously mark-

ed. Then shuffle and lay them again on the table, pronouncing that they will be then in alphabetical order. Appear to be surprised that you have failed; take them up again and give them a second shuffle, and then counting them down on the table they will all be in their natural order.

RECREATION XXXII.

Several letters being wrote promiscuously upon 32 cards, after they have been once shuffled, to find in a part of them a question; and then shuffling the remainder a second time, to shew the answer.

SUPPOSE the question to be, What is each Briton's boast? and the answer, His Liberty; which taken together contain 32 letters.

After you have wrote those letters on 32 cards, write on a paper the words his liberty,

liberty, and annex to the letters the first ten numbers thus:

HIS LIBERTY

1 2 3 4 5 6 7 8 9 10

Then have recourse to the table of combinations for ten numbers, and apply the respective numbers to them in the same manner as in the 30th Recreation, taking the first column, as these are to be shuffled only once, according to that order.

123 45678910 IBS LERTHIY

This is the order in which these cards must stand after the whole numbers 32 has been once shuffled, so that after a second shuffle they may stand in their proper order. Next dispose the whole number of letters according to the first column for 32 letters: the last ten are to be here placed in the order above; as follows,

WHAT IS EACH BRITON'S
1 2 3 4 56 7 8 9 10 11 12 13 14 15 16 17

B O A S T?

I B S L E R T H I Y 23 24 25 26 27 28 29 30 31 32

Therefore

Therefore, by the first column of the table, they will next stand thus:

You must observe that the card here placed the 16th in order, being the last of the question, is a long card; that you may cut them, or have them cut, after the first shuffle, at that part, and by that means separate them from the other ten cards that contain the answer.

Your cards being thus disposed, you show that they make no meaning; then shuffle them once, and cutting them at the long card, you give the first part to any one, who reads the question, but can find no answer in the others, which you open before him; you then shuffle them a second time, and shew the answer as above.

RECREATION XXXIII.

To write 32 letters on so many cards, then shuffle and deal them by twos to two persons, in such manner, that the cards of one shall contain a question, and those of the other, an answer.

SUPPOSE the question to be, Is nothing certain? and the answer, Yes, difapointment.

Over the letters of this question and answer write the following numbers, which correspond to the order in which the cards are to be dealt by two and two.

IS NOTHING CERTAIN
31 32 27 28 23 24 19 20 15 16 11 12 7 8 3 4
YES DISAPOINTMENT
29 30 25 26 21 22 17 18 13 14 9 10 5 6 1 2

Then have recourse to the first column of the table for 32 numbers, and dispose

pose these 32 cards in the sollowing order, by that column.

OIERGCANT PINTAIS

17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32

TMEHSDINNOYNTEIS

The cards being thus difposed, shuffle them once, and deal them 2 and 2; when one of the parties will necessarily have the question, and the other the answer.

Inftead of letters you may write words upon the 32 cards, 16 of which may contain a question, and the remainder the answer; or what other matter you please. If there be found difficulty in accommodating the words to the number of cards, there may be two or more letters or fyllables wrote upon one card.

RECREATION XXXIV.

The Five Beatitudes.

The five bleffings we will suppose to be, 1. Science, 2. Courage, 3. Health, 4. Riches, and 5. Virtue. These are to be found upon cards that you deal, one by one, to five persons. First write the letters of these words successively, in the order they stand, and then add the numbers here annexed to them.

SCIENCE COURAGE
31 26 21 16 11 6 1 32 27 22 17 12 7 2
HEALTH RICHES
28 23 18 13 8 3 29 24 19 14 9 4
VIRTUE
30 25 20 15 10 5

Then range them in order agreeable to the first column of the table for 32 numbers, as in the last Recreation. Thus.

I 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
LHNATEREUACRGTIU
17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32
FECIICHSOHREEVSC

Next, take a pack of cards, and write on the four first the word Science; on the four next the word Courage; and so of the rest.

Matters being thus prepared, you shew that the cards on which the letters are wrote convey no meaning. Then take the pack on which the words are wrote, and spreading open the first four cards, with their backs upward, you desire the first person to choose one. Then close those cards and spread the next four to the second person; and so to all the five; telling them to hold up their cards lest you should have a confederate in the room.

You then shuffle the cards and deal them one by one, in the common order, beginning with the person who chose the first card, and each one will find in his hand the same word as is wrote on his card. You will observe, that after the fixth round of dealing, there will be two cards Vol. I. He left

left, which you give to the first and second persons, as their words contain a letter more than the others.

RECREATION XXXV.

The cards of the game of piquet being mixed together, after shuffling them, to bring, by cutting them, all the cards of each suit together.

HE order in which the cards must be placed to produce the effect desired, being established on the same principle as that explained in the 31st Recreation, except that the shuffling is here to be repeated three times, we think it will be sufficient to give the order in which they are to be placed before the first shuffle.

Order of the Cards.

1 Ace 2 Knave clubs 3 Eight 4 Seven wide card	17 King clubs 18 Ten 19 Nine hearts 20 Seven clubs
7 Ten clubs6 Eight } fpades.7 Seven } fpades.wide card	21 Ace diamonds 22 Knave fpades 23 Queen hearts
7 Ten 9 Nine 10 Queen 11 Knave 12 Queen clubs 13 Eight	24 Knave hearts 25 Ace fpades 26 King diamonds 27 Nine clubs 28 Ace 29 King } hearts
13 Eight Seven hearts wide card Ten fpades Nine	30 Eight clubs 31 King 32 Queen } fpades

You then shuffle the cards, and cutting at the wide card, which will be the seven of hearts, you lay the eight cards that are cut, which will be the suit of hearts, down on the table. Then shuffling the remaining cards a second time, you cut at the

I

fecond wide card, which will be the feven of spades, and lay, in like manner, the eight spades down on the table. You shuffle the cards a third time, and offering them to any one to cut, he will naturally cut them at the wide card*, which is the seven of diamonds and consequently divide the remaining cards into two equal parts, one of which will be diamonds and the other clubs.

RECREATION XXXVI.

The cards at piquet being all mixed together, to divide the pack into two unequal parts, and name the number of points contained in each part.

Queen and knave shall count, as usual, the ace I, and the other cards ac-

^{*} You must take particular notice whether they be cut at the wide card, and if they are not, you must have them cut, or cut them again yourself.

cording to the number of the points. Then dispose the cards, by the table for 32 numbers, in the following order, and observe that the last card of the first division must be a wide card.

Order of the cards before shuffling.

1 Seven hearts 17 Nine diamonds 2 Nine clubs 18 Ace spades 3 Eight hearts 19 Ten clubs 4 Eight 20 Knave 5 Knave { fpades 6 Ten } 21 Eight \ diamonds 22 King 7 Queen 8 Ace clubs 23 Seven spades 24 Seven diamonds
25 Queen 9 Ace hearts wide card 10 Nine hearts 26 Knave hearts 27 King clubs 11 Queen spades 12 Knave clubs 28 Nine 1 29 King . 13 Ten diamonds 14 Ten 30 Ace diamonds hearts 31 Seven clubs 15 King 16 Queen

You then shuffle them carefully, according to the method before described, and they will stand in the following order.

Cards.	Numb	ers.	Cards.	Numb	crs.
1 Nine		9	6 Ten c	Brought up lubs	34
1 Nine 2 King }	Spades	10	7 Ten d	iamonds	IO
3 Seven)		' 7	3 Ten h	earts	IO
4 Seven d	iamonds	7	9 Ace c	lubs	1
5 Ace spa	des	I	10 Ace he	earts (wide ca	rd) 1
Car	ried up	34		Total	66
			E	rought up	101
11 Eight H	Hearts	. 8	22 Queen	n hearts	10
12 Eight sp	pades	8	23 Nine)	9
13 Seven h		7	24 Knave		IO
14 Nine cl		9	25 Eight	> Diamond	.s 8
15 Knave 7	Spades	IO	26 King	a management of the control of the c	IÒ
16 Ten	Spaues	IO	27 Quee:	n j	IO
17 Queen	clubs	10	28 Knave	e hearts	10
18 Nine he	earts	9	29 King	clubs	10
19 Queen	fpades -	10	30 Ace d	iamonds	Ţ
20 Knave o	clubs	10	31 Seven 32 Eight	Clube	7
21 King h	earts	10	32 Eight	Citios	8
Carr	ied up	101		Total	194

When the cards are by shuffling disposed in this order, you cut them at the wide card, and pronounce that the cards you have cut off contain 66 points, and consequently the remaining part 194. This recreation excites a good degree of admiration, but the applying of these cards to the next Recreation produces a much greater.

RECREATION XXXVII.

The inconceivable repique*

HEN you would perform this Rccreation with the cards used in the last, you must observe not to disorder the first ten cards in laying them down on the table. Putting those cards together, in their proper order, therefore you shuffle them a fecond time in the fame manner, and offer them to any one to cut, observing carefully if he cut them at the wide card, which will be the ace of hearts, and will then be at top; if not you must make him, under some pretence or other, cut them till it is; and the cards will then be ranged in fuch order that you will repique the perfon against whom you play, though you let him choose (even after he has cut) in what fuit you shall make the repique.

^{*} This manœuvre of piquet was invented by the Counters of L--- (a French lady), and communicated by her to M. Guyot.

Order of the cards after they have been shuf-.
fled and cut.

3 Knave Spades 1 4 Ten 2 5 Queen 6 Knave 2 7 King 8 Queen 2 9 Eight 2 10 King 4 diamonds 2 11 Queen 2 12 Ace 2 13 Seven 14 Eight 3 15 Knave hearts 3	7 Nine 8 Knave 9 Nine hearts 9 Nine hearts 0 Queen fpades 1 Seven hearts 2 Nine clubs 3 Ten hearts 4 Ace clubs 5 Seven fpades 6 Seven diamonds 7 Nine 8 King 9 Ace 9 Ten clubs 1 Ten diamonds 2 Ace hearts
	2 Ace hearts (wide card)

The cards being thus disposed, you ask your adversary in what suit you shall repique him. If he say in clubs or diamonds you must deal the cards by threes, and the hands will be as follows:

Elder.	Younger.
Hearts, king	Clubs, ace
queen	king
—— knave	—— queen
nine	knave
eight	— nine
feven	Diamonds, ace
Spades, queen	king
knave	queen
eight	knave
Diamonds, eight	nine
Clubs, eight	Spades, ten
feven	Hearts, ten

of the elder. Seven spades Seven diamonds Nine) King \ fpades

Rentree, or take in, Rentree of the younger. Ten clubs Ten diamonds Ace hearts

If he against whom you play, who is fupposed to be elder hand, has named clubs for the repique, and has taken in five cards, you must then lay out the queen, knave, and nine of diamonds, and

you will have, with the three cards you take in, a fixiem major in clubs, and quatorze tens. If he leave one or two cards, you must discard all the diamonds.

If he require to be repiqued in diamonds, then discard the queen, knave and nine of clubs; or all the clubs if he leave two cards; and you will then have a hand of the fame strength as before.

Note, If the adversary should discard five of his hearts, you will not repique him, as he will then have a feptiem in fpades: or if he only take one card: but neither of these any one can do, who has the least knowlege of the game. If the person against whom you play would be repiqued in hearts or spades, you must deal the cards by twos, and the game will fland thus:

Elder hand.

Younger hand.

King
Knave
Nine
Eight
Queen
Knave
Nine
Seven
Eight
Seven
Light
Sev

Ace King | clubs |
Ace Queen | diamonds |
Queen Knave | fpades |
Ten King Queen |
Knave | hearts |
Ten Nine |

Rentree.

Seven fpades
Seven diamonds
Nine
King
Ace
fpades

Rentree.

Ten clubs Ten diamonds Ace hearts

If he require to be repiqued in hearts, you keep the quint to a king in hearts, and the ten of fpades, and lay out which of the rest you please: then, even if he should leave two cards, you will have a fixiem major in hearts, and quatorze tens, which will make a repique.

But if he demand to be repiqued in fpades; at the end of the deal you must dextrously pass the three cards that are at the bottom of the stock (that is, the ten of clubs, ten of diamonds, and ace of hearts) to the top*, and by that means you reserve the nine, king, and ace of spades for yourself: so that by keeping the quint in hearts, though you should be obliged to lay out four cards, you will have a sixiem to a king in spades, with which and the quint of hearts, you must make a repique.

Observe here likewise, that if the adversary lay out only three cards, you will not make the repique: but that he will never do unless he be quite ignorant of the game, or has some knowledge of your intention.

This last stroke of piquet has gained great applause, when those that have

^{*} The manner of doing this you will find in the Appendix, among the Recreations of Dexterity.

publicly performed it, have known how to conduct it dextrously. Many persons who understand the nature of combining the cards, have gone as far as the passing the three cards from the bottom of the stock, and have then been forced to confess their ignorance of the manner in which it was performed.

RECREATION XXXVIII.

The metamorphofed Cards.

PROVIDE thirty-two cards that are differently coloured; on which feveral different words are wrote, and different objects painted. These cards are to be dealt two and two, to four persons, and at three different times, shuffling them each time. After the first deal every one's cards are to be of the same colour: after the second deal, they are all to have objects that are similar; and after the third, words that convey a sentiment.

Dispose of the cards in the following order.

Order of			*
the cards.	Colours.	Objects.	Words.
I	Yellow	Bird	I find
2	Yellow	Bird	In you
3 .	Green	Flower	Charming
4	Green	Flower	Flowers
	White	Bird	To hear
5 6	White	Orange	Beauty
7	Red	Butterfly	My
7 3	Red	Flower	Notes
9	Red	Flower	In
10	Red	Butterfly	Shepherdefs
H	Green	Butterfly	Lover
12	Green	Butterfly	Your
13	White	Flower	Of
14	White	Flower	an inconstant
15	Yellow	Orange	Image
16	Yellow	Flower	Inchanting
17	White	Orange	Ardor
81	Yellow	Butterfly	My
19	Yellow	Butterfly	Phyllis
20	White	Bird	Birds
2 I	Red	Orange	Sing
22	Red	Orange	Dear
23	Green	Orange	and Sweetness
24	Green	Orange	The
25	Green	Bird	Of
U			

Order of			
the cards.	Colours.	Objects.	Words.
26	Green	Bird	Prefent
27	Yellow	Flower	As
28	Red	Bird	Changes
29	Red	Bird	Bofom
30	Yellow	Orange	Mc
31	White	Butterfly	Your
32	White	Butterfly	Ilong

The cards thus coloured, figured, and transcribed, are to be put in a case, in the order they here stand.

When you would perform this Recreation you take the cards out of the cafe, and show, without changing the order in which they were put, that the colours, objects, and words are all placed promiscuously. You then shuffle them in the same manner as before, and deal them, two and two, to four persons, observing that they do not take up their cards till all are dealt, nor mix them together: and the eight cards dealt to each person will be found all of one colour. You then take

each person's cards, and put those of the fecond person under those of the first, and those of the fourth person under those of the third. After which you shuffle them a fecond time, and having dealt them in the fame manner, on the first person's cards will be painted all the birds; on the fecond person's cards, all the butterflies; on those of the third, the oranges; and on those of the fourth, the flowers. You take the cards a fecond time, and observing the fame precautions, shuffle and deal them as before, and then the first person, who had the last time the birds in his hands, will have the words in his hand that compose this sentence.

Sing dear birds, I long to hear your enchanting notes.

The fecond person, who had the last deal the butterflies, will now have these words,

Of an inconstant lover your changes present me the image.

The third, who had the oranges, will have this fentence.

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As in my Phylis, I find in you, beauty and sweetness.

The fourth, who had the flowers, will have these words,

Charming flowers, adorn the bosom of my sheperdess.

It feems quite unnecessary to give any farther detail, as they who understand the foregoing Recreations will easily perform this.

RECREATION XXXIX.

The repique with carte blanch.

IN the following Recreations relating to piquet, we shall confine ourselves to the order in which the cards must stand after they are cut, and ready to be dealt. They who chuse to shuffle them first (in order to make the performance appear the more extraordinary) may easily dispose them in a proper order for that purpose, by having recourse to the table of combinations for 32 numbers.

I

Vol. I.

Order of the cards.

Ace Seven Spades Elder

Younger 3 Seven clubs 4 Ten hearts

E. 5 Ace hearts 6 Knave fpades

Y. 7 Nine hearts 8 Eight clubs

E. 9 Queen fpades
Lo Ace diamonds

Y. 11 Eight hearts 12 Eight fpades

E. 13 Queen diamonds 14 Ace clubs

Y. 15 Nine diamonds 16 Nine clubs

E. 17 King | Diamonds

Y. 19 Seven hearts 20 Seven diamonds

E. 21 Nine fpades 22 Knave diamonds

Y. 23 Ten clubs 24 Eight diamonds

25 King hearts 26 King clubs 27 Queen hearts Eldei's rentrée 28 King spades 29 Ten spades 30 Queen clubs 31 Knave clubs Younger's rentrée 32 Knave hearts

The cards being thus disposed, the hands of the players, after they have been dealt two and two, will be as follows.

Elder. Younger. Ace Ten Nine Eight Queen Knave | Spades Nine Seven Seven Ten Ace Nine King Queen diamonds Seven Knave Nine Ten / Eight Diamonds Ace hearts Seven) Ace clubs Eight spades

The Rentrée.

King Queen (Knave) hearts Queen King clubs Knave hearts King **fpades** Ten

The cards being thus dealt, you defire the other player to cast his eye over the two hands, and take which he please, on condition, that if he keep the hand dealt him he shall be eldest; but if he take the other he shall be youngest.

If he keep the hand dealt him, which in appearance is much preferable to the other, he will naturally lay out the four lowest spades, and leave a card, by carrying the quint in diamonds and four aces. You then tell down your carte blanch, and keeping the two quarts in clubs and hearts, lay out the others, and with your rentrée you will have a fixiem in clubs and a quint in hearts, with which you will make a repique, counting 107 points, though if the cards were played you would be capoted.

If the opposite player choose the youngest hand, you then discard the quart to a king in diamonds with the seven of spades

fpades, and with your rentrée you will have a fixiem major in spades, and quatorze of aces: by which you make repique and capot.

Here also you may miss the repique, if the other player keep the hand dealt him, and difcard his diamonds; but this as in the other cases, no one will do, who has any knowledge of the game.

RECREATION XL.

Case at piquet, where you repique the elder hand, though he have the choice of the cards after they are dealt.

THE cards must here stand, after they have been cut, in the following order.

> Elder Ace 2 Eight } fpades

Younger 3 Knave 1 clubs

E. 5 Ace clubs Nine hearts

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Y. 7 Eight clubs 8 Nine diamonds

E. 9 Queen clubs 10 Eight diamonds

Y. 11 Seven clubs 12 Ten diamonds

E. 13 Ten Spades 14 Eight hearts

Y. 15 Nine clubs

E. 17 King | fpades

Y. 19 Knave diamonds 20 Seven fpades

E. ²¹ Seven diamonds 22 Knave fpades

Y. ²3 Ace diamonds ²4 Nine fpades

> 25 King 26 Knave

Rentrée E.27 Queen hearts 28 Seven 29 Ten

30 Ace hearts

Rentrée Y.31 Queen } diamonds

The cards being thus disposed * when they are dealt, the hands of the two players will be as follows.

CIS WIII DO AS TOLLOWS					
Elder.	Younger.				
Spades, ace	Diamonds, ace				
king	——— knave				
—— queen	— ten				
knave	nine				
——ten	Clubs, king				
eight	— knave				
Clubs, ace	— ten				
queen	— nine				
Hearts, nine	eight				
eight	—— feven				
Diamonds, eight	Spades, nine				
feven	—— feven				
Rentrée.	Rentrée.				
King	Ace, hearts				
Queen	King Ldiamonda				
Knave hearts	King Queen diamonds				
Ten					
Seven j					

You then give the other player the liberty of choosing either hand, but without

I 4 feeing

^{*} In all these Recreations with piquet, there should be a wide card last, that they may be properly cut.

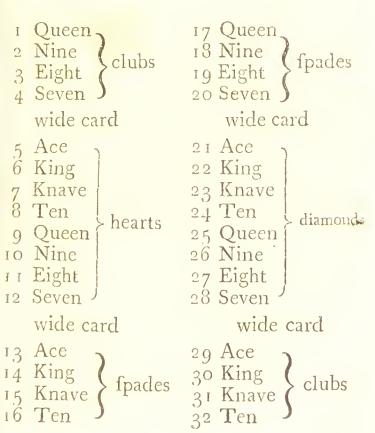
feeing them. If he chofe the elder hand, you discard the king of clubs, with the nine and seven of spades, and by your rentrée you will have a fixiem in diamonds and the point which will make 22, and that added to the quint in clubs will make 97, and you will necessarily win, as the adversary will not fail to lay out his two small hearts.

If, on the contrary, he choose the younger hand, you discard the knave, ten and eight of spades, with the seven and eight of diamonds: then by taking in the quint to a king in hearts, you will have a septiem in hearts, a tierce major in spades, and three queens, which will tell 90, though the adversary should discard to the most advantage possible.

RECREATION XLI.

Case at piquet, where you give the other player or not only the choice of the suite in which he will be repiqued, but that of dealing the cards by twos or by threes, and of taking either hand after they are dealt, you being to tell and play first.

THE cards must be disposed as follows:

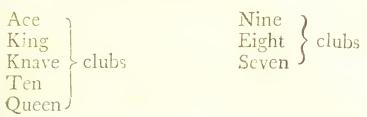


It is evident by this disposition of the cards, that if they are cut at any one of the wide cards, which are the last of each suite, there will be always a stock of eight cards of the same suite. Consequently, if he with whom you play require to be repiqued in clubs, by cutting at the first wide card, which is the seven of clubs, the eight clubs will necessarily be at the bottom of the pack, and you will have for your rentrée a quint major in clubs. The same will happen in all the other suites, by cutting at the 7 of each. If he deal the cards by twos, the hands will be as follows*.

Elder	Younger
Ace King Queen Nine hearts	Ten Eight Seven Knave hearts
Ace King Queen Nine fpades	Knave Ten Eight Seven Knave fpades
Ace King Queen diamonds Nine	Knave Ten Eight Seven diamonds

^{*} The hands will be always the fame, though in different fuites.

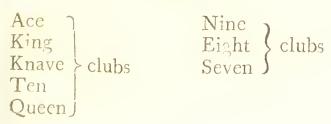
Rentrée



But if he deal the cards by threes, the hands will fland thus:



Rentrée.



If the other player require to be repiqued in spades, you cut them at the 7 of that suite, and tell him he is at liberty to deal them by twos or threes*. If he deal them by twos, he is to choose which hand he will have, without seeing them; you being still eldest.

If he keep his own hand, you discard the nine of hearts, spades and diamonds, and either of the two queens; and by your rentrée you will have a quint major in clubs, quatorze aces, and quatorze kings, with which you make a repique. But if he choose the cards dealt for the elder, you discard the seven of hearts, spades, and diamonds, and any two of the eights; and you will have by your rentrée the same quint in clubs, quatorze queens and quatorze knaves; which will also make a repique.

^{*} You are to take care he does not shuffle the cards; and the better to prevent it, you may so dispose them as to shuffle them before him, after the manner explained in some of the foregoing Recreations.

If the adversary deal the cards by threes, and keep his hand, you discard the king, eight and feven of hearts, with the nine and eight of spades; and by your rentrée you will have the quint major in clubs, a tierce to a queen in diamonds, three aces, three queens, and three knaves, with which you make a repique. But if he choose the cards dealt for the elder, you difcard the queen and nine of hearts, the knave and feven of fpades, and the ace of diamonds, and you will then have the fame quint in clubs, a tierce to a nine in diamonds, three kings and three tens, with which you will tell 29 points, therefore by playing one, you can in this cafe make a pique only.

RECREATION XLII.

An exemplary case at piquet, where you repique your adversary, after giving him the choice of having the cards dealt either by twos or threes.

O dispose the cards in the order necessary to produce the effect here required, and in all others where you give the choice of having the cards dealt either by twos or threes, you must have recourse to the following table.

Cards that will go to the eldeft.	Numb. of the Cards.	Cards that will come to the youngest.	Variable cards.
I Cos	(I)	youngen.	
2	$\left\{\begin{array}{c}1\\2\end{array}\right\}$		
)		
	3 }	4	3
		4	5
	5 6 1		5
	(7)		7
	{ 7 }		8
9	(9)		C (CLEAN
	(10)		IO WE
	{11}	I I	
	(12)	12	
13	(13)		
14 BB	3145		
	(151		15
	[16]	16	
	{ 17}		17
	(81)		18
	$\{19\}$		19
2'1	{20}		20
21	(21)		
	\(\(\) 22 \(\)		22
	${23}$	23	
	(24)	24	

This table shews the different hands that result from the two different methods of dealing the cards; that the eldest hand has always, in some order or other, the fix cards placed against the numbers, 1, 2, 9, 13, 14, and 21: and the younger, the fix cards placed against 4, 11, 12, 16, 23, and 24. It shows likewise, that the 12 cards marked 3, 5, 6, 7, 8, 10, 15, 17, 18, 19, 20, and 22, may be in either hand, so far as concerns the manner of dealing the cards.

Being therefore certain when you deal, that the cards marked 1, 2, 9, 13, 14, and 21 will always be in the adversary's hand, and those marked 4, 11, 12, 16, 23, and 24, will be in your own hand, you must apply your fix numbers to such cards, as with the three of the rentrée, (which you may choose as you please) will always make a great hand, and superior to the adversary. The great cards which you are forced to leave, you must distribute among the

the variable cards, in fuch manner that they can have no remarkable effect, when dealt either way.

This method we have observed in the following example, which we here give for the fatisfaction of those who would compose these sorts of games themselves. To the numbers 4, 11, 12, 16, 23, and 24, annex a fixiem major in hearts, which joined to the three tens of the rentrée are sufficient to make a repique, youngest hand. But as you must prevent the elder hand from defeating your point, by having feven cards in any of the other fuits, you are so to dispose some part of each fuit, by the column of variable cards, that he may never have, whether the cards are dealt by twos or threes, any large fequence*: as you will

^{*} If you cannot effect this by the cards that are to be dealt the adversary, you must so dispose his rentrée, that he may lay out his game, as in the thirty-eighth Recreation.

fee by the following difposition of the cards.

I	King)	17 Ace clubs
2	King Ace diamonds Nine	18 Seven 19 King 20 Ace fpades
3	Nine)	19 King Spades
4	Ace hearts	
5	Queen spades	21 Knave diamonds
6	Eight diamonds	22 Eight clubs
	Queen clubs	23 Ten \ hoorts
	Eight spades	23 Ten hearts land
	King clubs	
		25 Knave } fpades 26 Nine }
TI	Seven hearts	27 Knave clubs
12	Nine S	28 Eight hearts
T 2	Queen 1 1.	29 Nine clubs
TA	Seven \diamonds	29 Nine clubs 30 Ten diamonds
	Seven clubs	31 Ten spades
	Knave hearts	32 Ten clubs
1 ()	ALLEY V WALLEY TO A STATE OF THE STATE OF TH	

By this arrangement of the cards you will be fure to fucceed, whether you deal the cards by twos or threes: even though the adverfary, thinking to fruftrate your intention, should leave three cards.

Remark: there is no danger that any of these recreations at piquet should be applied to a bad purpose, for after the cards have been once shuffled by both players, it will be impossible to succeed in any one of them. There are, however, tricks to be played at this, as at all other games, with the cards; fuch as changing the whole pack, or fome particular cards, or taking in part, or all the discard, or making the pass, that is, bringing part of the cards at bottom to the top, as will be more fully explained in the fourth vol. all of which many persons can persorm so dextrously, that it is impossible for the eye to discover them. We fay nothing of the practice of marking the cards, for of that almost every one's experience will afford fufficient proof. To aggravate the misfortune, it is indubitably certain, that many perfons who are strictly honest in all other respects, are dishonest at cards; and that no rank or condition of men, no, nor woman neither, is entirely free from this vice.

K o

They

They who make a trade of dexterity frequently exhibit other recreations with the cards; but as those have no relation to numbers, they will be found among the miscellaneous articles in the Appendix to the last volume.

RECREATION XLIII.

Several different cards being shown to different persons, that each of them may fix on one of those cards, to name that on which each person fixed.

THERE must be as many different cards shown to each person, as there are persons to choose; therefore, suppose there are three persons, then to each of them you must show three cards, and telling the first person to retain one in his memory, you lay those three cards down, and show three others to the second person, and so to the third. You then take up the first person's cards, and lay them down, one by one, separately, with their faces

faces upwards. You next place the fecond person's card over the first, and in like manner the third person's card over the fecond's; fo that in each parcel there will be one card belonging to each perfon. You then alk each of them in which parcel his card is, and when you know that, you immediately know which card it is; for the first person's card will always be the first, the second person's the fecond, and the third person's the third, in that parcel where they each fay his card is.

This Recreation may be performed with a fingle person, by letting him fix on three, four, or more cards. In this cafe you must show him as many parcels as he is to choose cards, and every parcel must consist of that number, out of which he must fix on one; and you then proceed as before, he telling you the parcel that contains each of his cards.

RECREATION XLIV.

To name the rank of the card that a person has drawn from a piquet pack.

If Y the rank of the card we mean whether it be ace, king, queen, &c. You are therefore first to fix a certain number to each card, thus, you call the king 4, the queen 3, the knave 2, the ace 1, and the others according to the number of their pips.

You then shuffle the cards, and let the person draw any one of them: then turning up the remaining cards, you add the number of the first to that of the second, that to the third, and so on, till it amount to ten, which you then reject and begin again; or if it be more, you reject the ten, and carry the remainder to the next card; and so continue till you come to the last card; and to the last amount you must add 4, and subtract that sum from 10 if it be

less, or from 20 if it be more than 10, and the remainder will be the number of the card that was drawn: as for example, if the remainder be 2, the card drawn was a knave; if 3, a queen, &c.

RECREATION XLV.

To tell the amount of the numbers of two cards that a perfon has drawn from a common pack of cards*.

THE small cards here tell, as before, according to the number of their pips, but each pictured card tells for 10. Let the person add as many more cards to each of those he has drawn, as will make each of their numbers 25. Then take the remaining cards in your hand, and seeming to search for some card among them, tell them over to yourself, and their

^{*} This Recreation may be made with two persons, by letting each of them draw, and adding the numbers together.

number will be the amount of the two cards drawn. An example will make this plain. Suppose the person has drawn a 10 and a 7, then he must add 15 cards to the first, to make the number 25, and 18 cards to the last, for the same reason: now 15 and 18 make 33, and the two cards themselves make 35, which deducted from 52 leaves 17, which must be the number of the remaining cards, and also of the two cards drawn.

This Recreation may be performed without your touching the cards, thus: let the perfon who has drawn the two cards deduct the numbers of each of them from 26, which is half the number of the pack, and after adding the remainders together, let him tell you the amount, which you privately deduct from 52, the number of all the cards, and the remainder will be the amount of the two cards. For example, suppose the two cards to be, as before, 10 and 7; then the person deduct-

ing 10 from 26 there remains 16; and deducting 7 from 26 there remains 19; those two remainders added together will make 35, which you subtract from 52, and there must remain 17, for the amount of the two cards, as before.

As the number 26 may be thought to lead to a discovery of the principle on which the Recreation is founded, it being manifestly the half of the pack, to render it more mysterious you may take any other number less than 26, but greater than 10, as for example 24, and let the party fubtract the number of each of his cards from that; therefore, supposing the numbers to be as before 10 and 7, the remainders will be 14 and 17, which make 31, to which you must add 4, for the double of the 2 you took from 26, and the amount will be 35, which is to be deducted from 52, as before. By this alteration the performance will not only be rendered more abfrufe

struse, but also more diversified, as you may change the number, from which those of the two cards are to be deducted, every time you repeat the experiment.

This Recreation may be performed, equally well, with a pack of piquet cards, and then the numbers of the two cards must be deducted from 16, which is the half of the pack; or if you chuse to make it more mysterious, from any other number less than 16 and more than 10; afterwards adding, as in the last case, the double of what that number wants to make it 16.

RECREATION XLVI.

To tell the amount of the numbers of any three cards that a person shall draw from the pack*.

FTER the party has drawn his three cards, you are to draw one yourfelf, and lay it afide; for it is necessary that the number of the remaining cards be divisible by 3, which they will not be, in a pack of 52 cards, if only 3 be drawn. The card you draw you may call the confederate, and pretend it is by the aid of that card you discover the amount of the others. Then tell the party to add as many more to each of his cards, as will make its number 16, which is the third part of the remaining 48 cards; therefore, suppose he has drawn a 10, a 7, and a 6:

^{*} This Recreations may also be performed with three persons, but much more readily with one, as the separate additions and subtractions will be very like to occasion confusion.

then to the first he must add 6 cards, to the second 9, and to the third 10, which together make 25, and the 4 cards drawn being added to them make 29. You then take the remaining cards, and telling them over, as in the last Recreation, you find their number to be 23, which must be the amount of the three cards the person drew.

You may perform this Recreation like-wife without touching the cards, as thus: after the party has drawn his three cards, and you have drawn one, let him deduct the number of each of the cards he has drawn from 17, which is one-third of the pack, after you have drawn your card: and let him tell you the amount of the feveral remainders, to which you privately add one for the card you drew, and deducting that amount from 52, the whole number of cards, the remainder will be the amount of the three cards drawn. For example, suppose the three cards to

be 10, 7, and 6, as before; then each of those numbers being subtracted from 17, the remainders will be respectively 7, 10, and 11, which, added together, make 28, to which the fingle card you drew being <mark>added makes 29,</mark> and that number deduલed from 52 leaves 23, which is the amount of the three cards the party drew.

There is little reason to imagine any one will difcover why you here make choice of the number 17; but if you are defirous of rendering the Recreation still more abstruse, and at the same time susceptible of greater variety, you may fix on any other number less than 17, but more than 10; and afterwards add to the amount of the remainders the double of what that number is less than 17; in the same manner as in the last Recreation.

This Recreation also may be performed with a pack of piquet cards; but then you must draw, or, what will answer the

the fame purpose, deduct 2, in your own mind, from the whole number 32, that the remainder may be divisible by 3; and let him deduct the number of each of his cards from that sum, which is 10, and add the remainders together, as before; thus, if his three cards be 10, 7, and 6, he is to deduct each of them from 10, which is the third part of 30; therefore the remainders will be 0, 3, and 4, which, added together, make 7, and that added to the 2 you deducted from the whole number, makes 9, which taken from 32, leaves 23, and that must be the amount of his three cards.

Among the different purposes to which the doctrine of combinations may be applied, those of writing in cypher, and decyphering, hold a principal place, as will appear by the following Recreations.

DIFFERENT METHODS OF WRITING IN CYPHER.

The Lacedæmonians are faid to be the inventors of cyphers, or at leaft they were not, to our knowledge, ufed by any people before them. Their method was by a wooden cylinder or roller, called a Scytala Laconia, round which they rolled a thin parchment, and wrote their difpatches. It was then taken off and fent to the confederate, who had another roller, exactly of the fame fize, round which he wrapped the parchment, and read its contents.

RECREATION LXVII.

To communicate intelligence by a pack of piquet cards.

THE parties must previously agree in what manner the cards shall be first placed, and then how they shall be shuffled. Thus, suppose the cards are to be first placed in the order as hereafter follows,

and

and then shuffled by taking off 3 from the top, putting the next 2 over them, and the following 3 under them*, and so alternately. Therefore the party who sends the cypher first writes the contents of it on a separate paper, and then copies the first 32 letters on the cards, by writing one letter on every card; he then shuffles them in the manner described, and writes the second time and writes the shuffles them a second time and writes the third 32 letters, and so of the rest. An example will make this plain. Suppose the letter to be as follows:

I am in full march to relieve you; within three days I shall be with you. If the ene my in the mean time should make an assault, remember what you owe to your country, to your family and yourself. Live with ho nour or die with glory.

^{*} By shuffling the cards in this manner, there will remain only 2 to put under at last.

Seven

Order of the cards before the 1st shuffle.

	Ace spaces	i	а	d	u	y	i
	Ten diamonds	а	l	е	u	l	
	Eight hearts	m	l	m	0	i	26
	King spades	į	S	u	m	l	
	Nine clubs	n	h	l	e	0	
	Seven diamonds	f	b	m	r	i	
	Nine diamonds	и	е	a	С	t	n
	Ace clubs	l	w	k	r	y	i
	Knave hearts	l	S	e	е	а	e
	Seven spades	m	i	а	r	m	w
	Ten clubs	a	i	t	ħ	е	r
	Ten hearts	γ	r	h	0	f	
	Queen spades	С	h	\mathcal{C}	e	ī	
	Eight diamonds	h	а	h	y	ש	
	Eight clubs	t	y	0	0	0	l
	Seven hearts	0	y	а	0	h	0
	Queen clubs	r	0	n	u	y	h
	Nine fpades	е	u	i	у	f	y
	King hearts	l	е	t	С	u	0
	Queen diamond	s e	a	s	0	е	
	Eight fpades	ż	i	n	w	S	0
	Knave clubs	τ	j	a	n	t	g
7	ror I	T					

The person that receives these cards first places them in the order agreed on, and transcribes the first letter on every card. He then shuffles them, according to order, and transcribes the second letter on each card. He shuffles them a second time and transcribes the third letters; and so of the rest.

If the cards were to be shuffled the second time by threes and sours, the third time by twos and sours. &c. it would make the the cypher still more difficult to discover: though as all cyphers depend on the combination of letterss there are scarce any that may not be decyphered with time and pains; as we shall show farther on. Those cyphers are the best, that are by their nature most free from suspicion of being cyphers; as for example, if the letters were here wrote with one of the sympathetic inks, described in the fourth volume of this work, the cards might then pass for a common pack.

RECREATION XLVIII.

The mystical dial.

Na piece of square pasteboard ABCD (Plate II.) draw the circle EFGH, and divide it into twenty-fix equal parts, in each of which must be wrote one of the letters of the alphabet.

On the infide of this there must be another circle of pasteboard, ILMN, move-

able round the center O, and the extremity of this must be divided into the same number of equal parts as the other. On this also must be wrote the letters of the alphabet, which, however, need not be disposed in the same order. The person with whom you correspond must have a similar dial, and at the beginning of your letter you must put any two letters that answer to each other when you have fixed the dial.

Example.

Suppose you would write as follows:

If you will come over to us you shall have a pension, and you may still make a sham opposition.

You begin with the letters Ma, which show how the dial is fixed; then for If you, you write un juc, and so for the rest, as you will see at the bottom of the plate.

The fame intention may be answered by a ruler, the upper part of which is fixed and

and the lower part made to flide: but in this case the upper part must contain two alphabets in fuccession, that some letter of that part may constantly corréspond to one in the lower part. The divisions standing directly over each other in a ftraight line will be much more obvious than in the circumference of a circle. Or two straight pieces of pasteboard regularly divided, the one containing a fingle and the other a double alphabet, would answer exactly the fame purpose. In this case a blank space may be left at each end of the fingle alphabet, and one or two weights being placed on both the pieces will keep them fleady.

RECREATION XLIX.

The corresponding spaces.

TAKE two pieces of pasteboard or stiff paper, through which you must cut long squares, at different distances, as you will fee in the following example. One of thefe pieces you keep yourfelf, and the other L 3

other you give to your correspondent. When you would fend him any secret intelligence, you lay the pasteboard upon a paper of the same size, and in the spaces cut out, you write what you would have understood by him only, and then fill up the intermediate spaces with somewhat that makes with those words a different sense.

If shall be much obliged to you, as reading alone engages my attention at prefent, if you will lend me any one of the leight volumes of the Spectator. I hope you will excuse this freedom, but for a winter's evening I don't know a better entertainment. If I fail to return it soon, nevertrust me for the time to come.

A paper of this fort may be placed four different ways, either by putting the bottom at top, or by turning it over, and by those means the superfluous words may be

the more easily adapted to the sense of the others.

This is a very eligible cypher, as it is free from fuspicion, but it will do only for short messages: for if the spaces be frequent it will be very difficult to make the concealed and obvious meanings agree together; and if the fense be not clear, the writing will be liable to fufpicion.

RECREATION L.

The musical cypher.

THE construction of this cypher, is similar to that of the forty-eighth Recreation. The circle EFGH (Pl. III.) is to be divided into twenty-fix equal parts, in each part there must be wrote one of the letters of the alphabet: and on the interior circle ILMN, moveable round the center O, there is to be the fame number of divisions: the circumference of the inner circle must be ruled in the manner of a music a music paper, and in each division there is to be placed a note, different either in figure or position. Lastly, within the musical lines place the three keys, and on the outer circle, the figures that are commonly used to denote the time.

Then provide yourself with a ruled paper, and place one of the keys, as suppose that of ge re sol, against the time two-fourths at the beginning of the paper, which will inform your correspondent how to six his circle. You then copy the notes that answer to the several letters of the words you intend to write, in the manner expressed at the bottom of the plate.

A cypher of this fort may be made more difficult to discover by frequently changing the key, and that will not in the least embarrass the reader. You may likewise add the mark * or b to the note that begins a word, which will make it more easy to read, and at the same time give

the

Vol. 1.p 152. PLATE.III.



the music a more natural aspect. This cypher is preferable to that of the 48th Recreation, as it may be enclosed in a letter about common affairs, and pass unsuspected: unless it should fall into the hands of any one who understands composition, for he would very likely surmise, from the odd disposition of the notes, "that more is meant than meets the ear."

OF DECYPHERING.

The rules of decyphering are different in different languages: by observing the following, you will soon make out any common cypher wrote in English.

- n. Observe the letters or characters that most frequently occur, and set them down for the fix vowels, including y; and of these the most frequent will generally be e, and the least frequent u.
- 2. The vowels that most frequently come together are e a and o u.

3. The

- 3. The confonant most common at the ends of words is s, and the next frequent r and t.
- 4. When two fimilar characters come together, they are most likely to be the confonants f, l, or s, or the vowels e or o.
- 5. The letter that precedes or follows two fimilar characters is either a vowel, or l, m, n, or r.
- 6. In decyphering, begin with the words that confift of a fingle letter, which will be either a, I, o, or \mathfrak{S} .
- 7. Then take the words of two letters, one of which will be a vowel. Of these words the most frequent are, an, to, be, by, of, on, or, no, so, as, at, if, in, is, it, he, me, my, us, we, am.
- 8. In words of three letters there are most commonly two consonants. Of these words the most frequent are, the, and, not, but, yet, for, tho', how, why, all you, she, his, her, our, who, may, can, did, was, are, has, had, let, one, two, six, ten, &c*.
- * Some of these, or those of two letters, will be found in every sentence.

9. The

- 9. The most common words of four letters are, this, that, then, thus, with, when, from, here, some, most, none, they, them, whom, mine, your, self, must, will, have, been, were, four, five, nine, &c.
- 10. The most usual words of five letters are, there, these, those, which, were, while, fince, their, shall, might, could, would, ought, three, seven, eight, &c.
- 11. Words of two or more fyllables frequently begin with double confonants, or with a preposition; that is a vowel joined with one or two consonants. The most common double confonants are, bl, br, dr, fl, fr, gl, gr, ph, pl, pr, fh, fp, ft, th, tr, wh, wr, &c. and the most common prepofitions are, com, con, de, dif, ex, im, in, int, mif, par, pre, pro, re, fub, fup, un, &c.
- 12. The double confonants most frequent at the end of long words are, ck, ld, lf, mn, nd, ng, rl, rm, rn, rp, rt, fm, ft, xt, &c. and the most common terminations are, ed, en, et, es, er, ing, ly, son, sion,

fion, tion, able, ence, ent, ment, full, less, ness, &c.

We shall here give an example of a cypher wrote in arbitrary characters, as is commonly practifed.

EXXOO EXTID XTELXA STO. ITE + TO ICTO + LXEOISTO. OOXUCOCHEA V+E ECII. ESIN +U EXECUTED Q. LSEECHT T+ EXSCE+X CE CA CFOGULOXOFLO � FOTIOLE OCE/OX LICED. $\Delta + \lambda O \lambda O S \Gamma \Delta \Gamma + \Delta O \Gamma O$. YO S IOLLOX VY+XEIA O TOE DO DOO EKSE CE L+XOD LIX+X EXO KOSXE +X ΓΟΝΟΧ OSXO E+ Δ00 YA FISTO Y+XO.

The foregoing will be eafily decyphered by observing the rules; but when the characters are all placed close together, as in the following example, and as they always, fhould be, the decyphering is much more difficult.

LENOONEELFLLEXEST OSALCX VXX TV VSTOAO NXO OCN VVIOOXE+VX 3 LASXLIJ X3 LXCSAX+ XONU, TOX V. +XLT OOUTI VUSUEXESTO FOR DOSEX CX VVLOX L USOX E □ C2 □ U CX+N V GT2 □ QN □ 3 L ON ON 3 L TYN XONEGULETUXNLEXDE T⊕XOTOSOT ♦ □SXOTO L TNUX.

To decypher a writing of this fort, you must first look for those characters that most frequently occur, and set them down for the vowels, as before. Then observe the similar characters that come together; but you must remember that two such characters may here belong to two words. You are next to remark the combinations of two or three characters that are most frequent, which will be some of the words in the seventh and eighth of the foregoing rules; and by observing the other rules, you will infallibly discover, with time and attention, any cypher wrote on these principles*.

* When the words are wrote all close together, if the key to the cypher were to be changed every word, according to a regular method agreed on between the parties, as might be done by either of the methods mentioned in the 48th Recreation, with very little additional trouble, the writing would be then extremely difficult to decypher. The longer any letter wrote in cypher is, the more easy it is to decypher, as then the repetitions of the characters and combinations are the more frequent.

The

The following are the contents of the two foregoing cyphers; in which we have inverted the order of the words and letters, that they who are defirous of trying their talent at decyphering, may not, inadvertently, read the explanation before the cypher.

enil eno ton dna shtnom elohw eerht, suoidifrep dna leurc o. noituac & ecnedurp fo klat lliw uoy: on, rotiart, tcelgen & ecnereffidni si ti. yltrohs rettel a em dnes ot snaem emos dnif rehtie, traeh eht morf semoc ti taht ees em tel &, erom ecaf ym ees ot erad reven ro.

evlewt fo ruoh eht ta thgin siht, ledatic eht fo etag eht erofeb elbmeffa lliw sdneirf ruo lla. ruoh eht ot lautcnup eb: deraperp llew emoc dna, ytrebil ruoy niager ot, ylevarb eid ro. thgin eht si siht, su sekam rehtie taht, etiup su seodnu ro.

The method of corresponding by fignals being nearly related to that of cyphers, we shall here give two instances of the manner in which it may be performed.

RECREATION LI.

Visual Correspondence.

PROVIDE a circle of wood ABCD (Plate IV. Fig. 1.) of about four feet in diameter, and divide its circumference, which will be about 12 feet, into 25 equal parts. In one of these spaces cut an open fquare, and through each of the others cut one of the 25 letters of the alphabet. (I ferving for \mathcal{J} .) Over the spaces that are cut out paste a thin oiled paper.

On the top of a pole P (Fig. 2.) fixed to the ground or floor, place a frame of wood EF, in which there is to be an opening of the same fize with one of the divisions on the wheel. On the outfide of this open-

ing

ing let there be a door, by which it may be occasionally closed. To the pole let the wheel be fixed, at its center G, round which it must turn, and be placed at such a height that the letters on its circumference may answer to the hole in the frame. Behind that part of the wheel which is opposite the board, let there be fixed, on a stand, a strong light.

When you would communicate your intelligence, open the door on the outfide of the frame; then put that division of the wheel in which the fquare is cut, against the opening, and place the light behind it; that ferves for a fignal to your correspondent, which he answers by putting his wheel in the fame position*. What you intend to communicate being wrote on a paper and placed before you in a

Vor. I.

^{*} Where there is a frequent correspondence required, certain hours of the day should be fixed for observing the signal.

proper position, you turn the wheel round, till that division which contains the first letter of the first word come before the opening, and keep it there while you tell 4; you then turn the wheel, either backward or forward*, to the second letter and keep that before the opening the same time; and so of all the letters of that word; and between every word you place the vacant division before the opening, while you, in like manner, tell 4. When you have finished the whole of your intelligence, you shut the door of the frame, or withdraw the light.

If your correspondent be far off, as suppose two or three miles, or farther, you must be each provided with a telescope, of a size adapted to the distance between you.

^{*} There may be placed handles on different parts of the wheel as at a, b, c, d, by which it will be the more readily turned about.

Your apparatus should be placed some way within the room, that it may not be obvious to paffengers. It is evident, from the construction of this instrument, that it is full as well adapted for a correspondence by night as by day.

A machine of this fort may be constructed at a trifling expence, and will be found highly useful in many instances, as where two perfons live on the oppofite fides of a large river, or in a country where the roads are for a great part of the year impassable, &c. If you are fearful any person, beside your correspondent. should know what passes, instead of letters, you may use 24 characters, like those we have given in the last example of cyphers.

This invention may also be applied to public use, as to convey intelligence to the garrison of a town besieged; or where great difpatch is required; and in that M_2

cafe feveral machines may be placed at different distances, that may convey the intelligence to each other; and here the wheel may be of a much larger dimension. There is one circumstance, however, that will render this contrivance entirely useless, and that is a thick mist or fog; for in that case, let the light be as strong, and the letters as large as they may, it will be impossible to discern them at any considerable distance. How to maintain a correspondence in that situation, will be shown in the next Recreation.

RECREATION LII.

Auricular Correspondence.

N the top of a house, or any other building, fix two bells A and B, (Pl. IV. Fig. 3.) by the iron rod CD, that passes thro' their handles, from which there must hang two ropes that go to the room beneath. The weight

weight of the handles should be nearly equal to that of the bells, so that a small additional force applied to the ropes may draw them up. One of the bells must be much larger than the other, that there may be no difficulty in diftinguishing their founds

The letters of the alphabet are to be expressed by pulling of these bells, according to the following order; in which you are to observe, that the small figures denote the number of pulls of the leffer, and the numeral letters, those of the greater bell.

A	I	GıI	NIIII	ТИт
B	2	H 2 I	O 2 III	VII 2
C	3	I3I	РзIII	UII 3
D	I	KıII	QII	WIII
E	H	L ₂ II	R I 2	XIII 2
F	III	$M_3 II$	S I 3	YIII 3
				ZIIII

M 3

After

166 RATIONAL, &c.

After each letter you must stop while you tell 4, and at the end of each word you may, for greater distinction, pull both bells twice together.

The above combinations may be continued to what number you pleafe; fo as to take in the most common words, such as and, the, you, he, she, they, them, this, that, may, can, do, &c.

VOL. I. p. 166. PLATE IV. Fig. 1. p 160. Fig. 2. p 160. Fig. 3. n 164.



MECHANICS.



MECHANICS.

DEFINITIONS.

ECHANICS is that science which explains the properties of moving bodies, and of those machines from which they frequently receive their motion.

- 2. Gravity is that power by which every body naturally defcends toward the center of the earth.
- 3. The center of gravity, in a fingle body, is that point round which the feveral parts of the body, in every fituation, exactly balance each other, and confequently if that point be fuspended the body will remain at rest.
- 4. The center of gravity, in two or more bodies, is that point between them, from which the diffance of each is in proportion to the quantity of matter it contains. The lefs the matter the greater the diffance.

5. The

- 5. The Vis Inertiæ, or Inert Force, is that property in bodies, by which they result the power that endeavours to put them in motion.
- 6. The denfity of bodies is the quantity of matter they contain, compared with their magnitude or dimensions.
- 7. Elasticity is that property in bodies by which, when their parts are forced out of their natural state, they return to it again; and by which two moving bodies, after striking, recoil from each other.
- 8. Power, in mechanics, is the force by which any body is put in motion.
 - 9. Weight, is the body to be moved.
- pound: fimple motion is that which proceeds from one power only; and compound motion is that which proceeds from two or more powers, either at the fame time or in fuccession.
- round which one or more bodies move.

12. Velocity of motion, is the space passed over by a body in a given time.

13. Accelerated motion, is that which continually increases, and retarded motion is that which continually decreases.

14. The quantity of motion, or momentum of a moving body, arifes from its velocity multiplied into the quantity of matter it contains.

15. There are fix primary mechanic infruments, commonly called mechanic powers, which are (1.) the lever*, (2.) the balance, (3.) the pulley, (4.) the wheel and axis, (5.) the fcrew†, and (6.) the wedge: to which is fometimes added the inclined

* Levers are faid to be of the first, second, or third fort, according to the situation of the sulcrum F, as in Pl. V. Fig. 1, 2, 3; to which is added the bended lever, Fig. 4.

† There are feveral forts of fcrews used in machines, of which those of Fig. 8, and 9 Pl. V. are most common. In Fig. 8, the part AB is called the male screw, and CD the nut, or semale screw. The part AB (Fig. 9.) which is turned by the wheel CD, is called an endless screw, because, while the wheel goes, it turns incessantly.

plane:

plane: and of fome or all of these-every compound machine is composed. See Plate V.

- 16. A pendulum is any body suspended from a point, from which it oscillates or vibrates, as from a center; but is generally understood to be a ball suspended at the end of a string or wire.
- 17. That resistance which arises from the rubbing of the parts of a machine against each other, is called their friction.

APHORISMS.

- 1. Every body, whether at rest or in motion, will constantly continue in its present state, unless compelled to alter it by some external power.
- 2. All motion, whether changed or generated, is in proportion to the force impressed, and is made in the direction that force acts.
- 3. Action and re-action, that is, the impulses of two bodies on each other, are always

always equal, and in contrary directions.

- 4. In bodies not elastic, if one in motion strike against another at rest, they will both move in the direction of the first moving body; and the quantity of motion in both bodies will be the same as it was in the first before the stroke.
- 5. If one fuch body in motion, strike against another moving in the same direction, but with less velocity, they will both continue in that direction, and the quantity of motion in both bodies will continue the same.
- 6. When two fuch bodies, with equal quantities of motion, and moving in opposite directions, strike against each other, their whole motion will be destroyed, and they will remain at rest.
- 7. If two fuch bodies, with different quantities of motion, and moving in opposite directions, strike against each other, they will continue to move in the direction of that body which had the greatest

momen-

momentum, and the quantity of motion in both bodies, after the stroke, will be equal to the difference of their motions before it.

8. The force of action in elaftic bodies is twice as great as that of non-elaftic bodies; for the former strike each other not only by impulse, but by repulse; recoiling from each other after the stroke*.

9. The inert force of every body is in proportion to its denfity.

10. All bodies near the furface of the earth descendequal spaces in equal times †.

11. The velocity of falling bodies, in unrefifting mediums, is 16 feet the first

* In these aphorisms bodies are supposed to be perfectly elastic or non-elastic: in all other bodies they will hold true only in proportion to the degrees of their elasticity.

† This must be understood of such as are called heavy bodies; for in those that are light the resistance of the air makes a considerable difference. A bullet and a feather fall with very different velocities in the air, though in the exhausted receiver they descend together.

fecond,

fecond, nearly, and becomes continually accelerated in a regular progression.

- 12. In every pendulum all its vibrations in fmall arches, or parts of circles, are made in the fame time.
- 13. The times of vibrations in different pendulums, are as the fquare roots of their length*: therefore a pendulum of four feet will vibrate twice while one of 16 feet vibrates once.
- 14. The length of a pendulum that vibrates every fecond, will be 39 inches, nearly \uparrow , and one that vibrates twice in a fecond will be $9\frac{4}{5}$ inches.
- 15. Any body, in the form of a rod or staff, that is every where of equal density, as an iron rod, and that is one third longer than a pendulum, will vibrate in the same time as that pendulum.
 - 16. In the lever, where the power P

See page 2. definition 2.

[†] A pendulum of this fort is therefore a regular measure of time, and may be of use on many occasions.

Pl. V. Fig. 1.) and weight W are to each other reciprocally as their distances from the fulcrum F, they will be in equilibrio*.

17. The balance being a lever of the first kind, where the fulcrum is placed exactly between its two extremities, if two weights E, F, (Pl. V. Fig. 5.) be placed any where, at equal distances from the fulcrum, and the balance remain in equilibrio, those weights must be equal.

by a rope going over a fixed pulley, the weight and power will be equal: but if one end of the rope be fixed, and the pulley be moveable with the weight, then the power will be but half the weight.

19. In a combination of pullies, as A, B, C, D, (Pl. V. Fig. 6.) called a tackle of pullies, the power will be to the weight,

^{*} The lever is to be regarded as the origin of the other powers, feeing they all act in a fimilar manner, though in different directions,

as I to the number of ropes applied to the moveable pullies GD, that is, in this cafe, as I to 4.

- 20. In the wheel and axis, the power will be to the weight, as the diameter of the axis is to the diameter of the wheel.
- 21. When there is a combination of wheels and axles, the power will be to the weight, as the diameters of the axles multiplied into each other, is to the diameters of the wheels multiplied into each other.
- 22. In the forew, the power is to the weight, as the perpendicular distance between any two threads of the screw A B, (Pl. V. Fig. 8.) is to the circumference of the circle described by the power at C or D*.
 - 23. In the wedge, the power is to the weight or resistance, as half the length of the base CE (Fig. 10.) to its heighth EF.
 - 24. In the inclined plane, the power is

^{*} The screw has the peculiar advantage of suftaining a considerable weight, when once raised, though the power be taken away.

to the weight, as the height of the plane CD (Fig. 11.) is to its length A B.

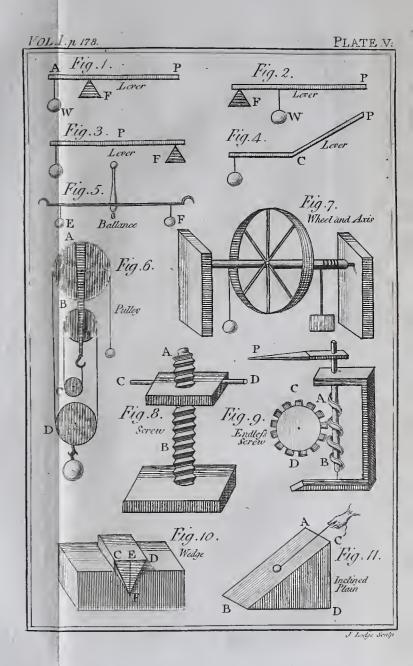
25. A body acquires the fame velocity by rolling down an inclined plane AB (Fig. 11.) as it would by falling through

its perpendicular height CD.

26. It is evident from the foregoing aphorisms, that whatever is gained in time is lost in power; and that no machine can of itself give any fresh power, but by diminishing the velocity of the weight, and increasing that of the power, bring them to an equality.

27. When a fly is added to any machine, as to a common jack, it does not increase, but diminish, the strength of the power; its only use being to regulate the motion of the machine, and keep it constantly equal*.

^{*} Though the fly does not in reality add any fresh power, yet by regulating the motion, it will in some cases, as when a man is employed to turn a large wheel, render the operation of the power more eafy and efficacious.





28. In every machine, when the weight and power are in equilibrio, the least additional power should put it and keep it in motion; but from the friction of the several parts of the machine, it is found that, on a medium, near one-third of the first power must be added to keep the machine in motion.

29. The friction of a machine does not arife merely from the number of the rubbing parts, but from the weight with which they are charged, multiplied into the velocity of the motion.

30. In all machines, fimplicity is their primary excellence, as they are thereby less liable to friction and impediment; the disorder of any one part of a machine frequently obstructing the operation of the whole.

RECREATION LIII.

To construct a mechanical dial without wheels, fpring, or weight.

HIS dial confifts of a tin or copper barrel or cylinder CD, (Plate VI. Fig 1.) which is supported by two strings of catgut that are fastened to the points A and B. This cylinder, for common use, may be about a foot long, and nine inches diameter.

The principal mechanism of this dial is in the internal structure of the cylinder which is represented by Fig. 2. and consists of five divisions*, that are formed by the five pieces af, bg, ch, di, and el, placed perpendicular to the ends of the cylinder: all these divisions must be precisely equal; and in each of the partitions

almost

^{*} There are fometimes fix or more divisions, and the machine is commonly efteemed the more accurate for having a greater number.

almost close to the circumference of the cylinder, there is to be a fmall hole, fuch as is made with a large needle.

In the divisions must be placed a quantity of water, equal to about one-fourth of the content of the cylinder; but the exact proportion can be determined by trial only. This water should be distilled, or at least well filtered, that it may not, by growing foul, impede the motion of the machine; and if there be a due quantity of spirits mixed with the water, it will be thereby prevented from freezing. At one end of the cylinder is a fmall hole, by which it may at any time be emptied; this hole is to be stopped with wax.

The barrel being brought up to the points A and B, by winding the firing round its axis, it would there rest, but the water oozing through the fmall holes in the upper partitions destroys its equilibrium; and as it flowly and gradually defends, the fmall points at the end of its axis show the hours, and parts of an hour, according to the number of divisions on the scales E or F.

If this dial go too fast or slow, it may be easily regulated, either by diminishing or increasing the size of the catgut, or the quantity of water in the cylinder.

Machines of this kind are most common in monasteries, and are frequently made by the monks themselves, for their own private use; the purchase of a watch requiring a sum of money which is very rarely possessed by any of that class of men; if they can be called men who disclaim the principal characteristic of manhood.

RECREATION LIV.

A dial to show the hour by gradually descending an inclined plane.

THE external structure of this dial confists of two parallel plates, connected by a hoop AB (Pl. VI. Fig. 3.) which is placed about one-eighth of an inch beneath the circumference of the plates. Thefe plates are indented, to prevent their fliding down the plane. On the front plate are inscribed the 24 hours; and at its center is a fmall hollow hemisphere g, moving freely on a pin: the lower part of this hemisphere is filled with lead, that keeps the little gentleman who fits upon it, and points with his finger to the hour, constantly in an erect position. The deep shades in the plate represent its concavity, which is about half an inch.

Fig. 4. in the same plate, represents the internal structure of this dial. LETQ

is the circumference of the hoop: f a frame-plate, on which is placed the train of wheels, 1, 2, 3, 4, which are nearly similar to those in another dial, and are, in like manner, governed by a balance and regulator. There is here no fpring, nor fusee, their effects being otherwise supplied, as will appear hereafter. The great wheel of the train is placed upon the axis of the movement, at the center, and the other wheels on one fide, which would give the machine a movement, for a short time, on a horizontal plane: it is therefore necessary to fix a thin plate of lead, C, on the opposite fide, to preserve the equilibrium. The machine will then rest in any position on the horizontal plane HH; but if it be placed on the inclined plane DGD, it will touch it in the point G, but cannot rest there; for the center of gravity at M, acting in the direction MT, and having nothing to support it, must necessarily descend, and carry the body down the plane.

But if on the other fide fuch a weight P. be fixed, as shall remove the center of gravity from M to V, in the line LG, which passes through the point G, then it will naturally rest on the inclined plane.

Now if the weight P be not fixed, but fulpended at the end of an arm or lever, which is fastened to the center-wheel I, moving on the axis of the machine at M, and which communicates, by its teeth, with the other wheels; in that case, if the weight P be just equal to the resistance arising from the friction of the train, the dial will remain at rest, as on a horizontal plane.

But if the weight P be superior to the resistance of the train, it will necessarily put it in motion, and the dial will then gradually descend the inclined plane; while the weight P, its arm PM, and the wheel 1, constantly preserve the same position

position they were in when the dial began to move,

From what has been faid it is eafy to conceive that the weight P may have fuch a determinate gravity as shall act upon the train with any required force, and confequently produce a motion in the machine of any required velocity, fuch, for example, as shall carry it round once in 24 hours. Therefore, if the diameter of the dial plate be four inches, it will describe the length of its circumference, that is, 12 inches five-tenths, nearly, in the 24 hours. From whence it follows, that this movement may be made to continue any number of days, by a proportional increase of the length of the plane; and if that were infinite, the motion of the dial would be perpetual.

The motion of this dial is eafily accelerated or retarded by raifing or depressing the inclined plane, by means of the screw S (Fig.

VOL. I. p 180. PLATE . VI. Fig. 2.p 180. Fig. 1. p 180. Fig. 4. L. 11 183. Fig. 3. A



S (Fig. 3.) The angle to which the plane is first raised is about 10 degrees, that is, the ninth part of a quadrant, or quarter of a circle.

RECREATION LV.

A clock to go perpetually by the influence of the celestial bodies.

THE conftruction of the movements in this clock is the fame with those in common use: it differs from those only in its situation, and the manner in which it is wound up.

This clock is to be placed near a wall, by, or against, which the tide constantly slows. To each of the barrels, round which the string that carries the weight is wound, there must hang a bucket, and into that, when the tide rises to a certain height, the water runs, by means of a pipe fixed in the wall. The bucket then overbalanceing the weight, descends, and winds up the clock;

clock; but when it comes to a certain depth, it is taken by a catch fixed in the wall, which, by turning it over, discharges the water. The weights of the clock then defcend in the ufual manner, and the buckets are drawn up.

Now as this clock is kept in motion by the tide, and as the tide proceeds from the influence of the fun and moon, it neceffarily follows, that the motion of the clock proceeds from the same cause; and that as long as the parts of the machine remain, motion will be perpetual.

This, according to the common, acceptation of the term, is certainly a perpetual motion; and fo is every mill that is driven by a constant stream; but that is not the fense in which the term was used by the advocates for a perpetual motion in the last century. They meant a machine, which, being once put in motion, should, by its peculiar construction, move perpetually,

tually, without any fresh force impressed. This they attempted by various means; as the attraction of a loadstone, the descent of heavy bodies, the difference of the momentum, in revolving weights, &c. all of which, though ingenious enough, discover a want of due attention to the principles of mechanics. Befides, if a perpetual movement could be effected by either of those means it would be of very little, or no use: for the unavoidable wear of the feveral parts of the machine, arifing from the incessant friction, must necessarily destroy that equality of motion, which alone could render its perpetuity of any consequence.

RECREATION LVI.

The Infcrutable lock.

THE difficulty a stranger would find in opening this lock, when in possession of the key, arises partly from the scutcheon that is placed before it, and partly from the peculiar form of the key.

The scutcheon AB (Pl. VII. Fig. 1.) consists of a circular plate of brassor iron, on whose rim are 24 teeth, that take the leaves of the pinion C: this scutcheon may therefore be placed in 24 different positions; in several, or all of which, the key may be inserted, but the lock opened in one of them only: D, is the aperture for the key, and a, b, c, d, are four knobs by which it is turned about.

The key ABCD (Fig. 2.) confifts of two fets of wards, which are divided into twelve

twelve parts, as is expressed by the parallel lines in the figure, and which should be made to join fo exactly, that when they are pressed together, their divisions may not be visible. At the middle of the key is a fcrew E, which, when turned in. fastens all the parts together, and when fcrewed out, fets them at liberty, that they may be turned round the barrel of the key, at the center of each part. When you have locked the door, you turn the fcutcheon about by one of the knobs; then unferewing the wards of the key, you turn part of them half round, that is, you bring fome of those parts that were next AB to CD, and then make them fast again, by the fcrew at the end.

Now if the person, into whose hands this key shall fall, be ignorant of the screw, it will be absolutely impossible for him to open the lock; and if he should know the use of it, the trials he must make before he can have any prospect of success.

cefs, will render the attempt highly abfurd; for there being 12 divisions in the key, it appears by the 18th Recreation of this volume, they may be placed in 479,001,600 different positions, and as each of these positions may be applied to the feveral ways in which the fcutcheon may be placed, it follows, that if the foregoing number be multiplied by 24, the product, which is 11,496,038,400, will be the number of all the trials that can be made: therefore, it is eleven thousand four hundred and ninety-fix millions, thirty-eight thousand, three hundred and ninety-nine, to one, at each trial, that he does not open the lock.

For common purposes a much less number may suffice: suppose, for example, there are only seven divisions in the key, the number of trials will be then 120,960. Now supposing 60 trials to be made in an hour, it would require 2016 hours to make all those trials, that is, to be sure of succeeding;

ceeding; that is, supposing again, a regular account to be kept of each trial as it is made, for otherwise the same trial might, and naturally would, be made several times.

RECREATION LVII.

So to dispose a hand-mill, to grind corn, &c. that being once put in motion, it shall work incessantly, from morning to night, without the assistance of any animal power.

THE form of this mill may be fimilar to those in common use: its motion is to be maintained by means of a smoke-jack: the use of this fort of jack is common enough; but its construction and manner of acting being clearly understood by few, we shall here describe them.

The horizontal wheel AB (Plate VII. Fig. 3.) is placed in the narrowest part of the chimney that is next the fire: its wings, which are made of tin, are inclin-Vol. I.

ed to the horizon, that is, placed in a floping direction. To the fame axis on which AB turns, is likewife placed the cog-wheel C, that takes the teeth of the perpendicular wheel D. On the fame axis with D, is placed the wooden wheel E, round which runs the rope F, on whose lower part is placed the wheel of the spit.

Now, the air, being rarefied by the fire, forces up the chimney, and meeting with the wings of the horizontal wheel in the narrowest port, necessarily turns it round, and at the same time turns the cog-wheel C, which turns D and E, together with the rope, which by its friction against the wheel of the spit, keeps that likewise constantly turning; and its velocity will be always in proportion to its weight, and the strength of the fire.

Therefore, if inflead of the iron spit, the handle of the mill be fixed in the center of the lower wooden wheel, it must, in like manner, turn that round: and the motion

VOL. I 11 10 1. PLATE VII. Fig. 1. A p 190. Fig. 3 . p. 193 .



motion will continue not only while the fire lasts, but a considerable time after; for there will be a continual circulation of the air up the chimney, till that in the room becomes equally cold with the external air.

This machine may in like manner be applied to the reeling of yarn; to the making a hammer strike perpetually on an anvil; and many other domestic purposes.

RECREATION LVIII.

A carriage to go without any other force than what it receives from the passengers.

THIS machine is represented by AB CD, (Pl. VIII. Fig. 1.) It is moved by the footman behind it; and the fore wheels, which act as a rudder, are guided by the person who sits in the carriage*.

* This machine was invented by M. Richard, a physician of Rochelle, and was exhibited at Paris in the last century. It is described by M. Ozanam in his Recreations Mathematiques.

Between the hind wheels is placed a box, in which is concealed the machinery that moves the Carriage. AA, Fig. 2. is a small axis, fixed into the box. B is a pulley, over which runs a rope, whose the two ends are fastened to the ends of two leavers or treddles CD, whose other ends are fixed in such manner in the piece E, which is joined to the box, that they can easily move up and down. FF are two slat pieces of iron, that are joined to the treddles, and take the teeth of the two wheels HH, which are sixed on the same axis with the hind wheels of the carriage, I, I.

It is evident that when the footman behind presses down one of the treddles, suppose C, with his foot, he must bring down one of the pieces of iron F, and confequently turn the wheel H that is next to it, and at the same time, by means of the rope that goes over the pulley, he must raise the other treddle D, together with its piece F, which being thrust down, will turn the other wheel H; and so alternate-

VOL.1.11 196. PLATE.VIII. Fig. 1.p. 195. Fig. 2 . 1106.

J. Lodge Scul



ly: and as the great wheels are fixed on the fame axis, they must necessarily move at the same time.

It is eafy to conceive that if the ends of the treddles next E, instead of being placed behind the carriage were turned the opposite way, so as to come under the feet of the person who sits in it, he might move it with equal, or even greater facility, than the footman, as it would then be charged with the weight of one person only.

A machine of this kind will afford a falutary recreation in a garden, or park, or on any plain ground, but in a rough or deep road must be attended with more pain than pleasure.

RECREATION LIX.

The catapulta.

THIS engine was in great repute among the ancients, and used by them in throwing darts or spears against their enemies, from whence it had its name. Some of the spears or darts thrown by these engines are said to have been eighteen feet long, and to have been thrown with such velocity as to take fire in their course*.

* It will not be improper to infert here, what is related by writers of the last century concerning the force of darts or arrows. Greaves, in his Pyromodographia, says, "Some Turkish bows are of "that strength as to pierce a plank six inches thick." He adds, "I speak what I have seen." And Barclay, a writer of sufficient credit, in his Icon Animorum, speaking of the Turkish bow, which differed very little in form from the long low bow, anciently in use among us, being drawn by the hand, without the help of the rack that is used to some other bows. He says, "I was an eye witness, "how one of these bows, with a little arrow, did pierce through a piece of steel three singers "thick."

ABCD, (Pl. IX. Fig. 1.) is the frame that holds the darts or arrows, which may be of different numbers, and placed in different directions. EF, is a large and ftrong iron fpring, which is bent by a rope that goes over the three pullies I, K, L, and is drawn by one or feveral men; this rope may be fastened to a pin at M. The rope therefore being fet at liberty, the fpring must strike the darts with great violence, and fend them with furprifing velocity to a great distance. This instrument differs in some particulars from the description we have of that of the ancients; principally in throwing of feveral darts at the fame time, one only being thrown by their's. A machine of this fort would be of use in those countries where there are frequently large flights of birds, for a great

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[&]quot;thick." Of facts like these a man may be very well allowed to doubt, or to suppose they were attended with some deception: yet totally to disbelieve them, when related by such witnesses, merely because they are to us impractible, savours rather of ignorance and temerity than a rational caution.

number of arrows being thus discharged at the same instant, could not fail of doing remarkable execution.

RECREATION LX.

To sail as fast, with a fair wind, by land as by water.

HIS is to be effected by means of a failing chariot, or boat fixed on four wheels; as AB (Plate IX. Fig. 2.) which is driven before the wind by the fails CD, and guided by the rudder E. In a chariot of this kind the wheels should be farther asunder, and the axle-trees longer, than in other carriages, to prevent overturning.

A machine of this fort was constructed in the last century by Stephinus, at Scheveling in Holland, and is celebrated by many writers. Its velocity with a strong wind is said to be so great, that it would carry eight or ten persons from Scheveling to Putten, which are forty-two English miles distant, in two hours.

Carriages

VOL.L. n 200. PLATE.IX. Fig. 1. p 199. Fig. 2. 1200.



Carriages of this kind are faid to be frequent in China; and in any wide, level country, must be sometimes both peasant and profitable. The great inconvenience attending this machine is, that it can only go in the direction the wind blows: and even not then unless it blows strong; so that, after you have got fome way on your journey, if the wind should fail, or change you must either proceed on foot, or go back. Some remedy for this inconvenience will be found in the next recreation. The Hollanders have, or had, fmall veffels, fomething of this kind, that carry one or two perfons on the ice, having a fledge at bottom inftead of wheels; and being made in the form of a boat, if the ice break the passengers are fecured from drowning.

RECREATION LXI.

To fail by land against the wind.

body of a failing chariot: M the mast, to which are fixed the wings or sails EFGH; the two first of which EF, are here supposed to be expanded by the wind. R is the rudder by which it is guided. Therefore the wind driving the sails round, with the mast M, and the cog wheel K, take the teeth, placed perpendicular to the sides of the two fore wheels of the carriage, and consequently keep it in continual motion.

The body of this machine should not be large, nor placed very high, not only to prevent overturning, but that its motion may not be thereby impeded; for the velocity will be in proportion to the force of the wind on the sails to that on the body of the machine. Therefore if they

be both equal it will stand still; or if the force on the body be the greatest, it will go backwards; unless there be a contrivance to lock the wheels. The upper part of the machine next A, may be made to take off, when the wind is contrary, and there may be another fet of fails placed between the two hind wheels, which will confiderably increase its velocity. But after all, for general use, a common carriage must be preferable; for this cannot be expected to go up a moderate ascent without great difficulty, nor down a declivity, when there is a strong wind, without danger; and even on level ground, if the road be in any degree rough, its progress must be very flow, attended both with difficulty and danger. In an open country, however, where there is a large tract of level and smooth ground, and frequent strong winds, a machine of this fort will certainly be very convenient; and in most countries, when made of a small fize, may be useful to young people, by affording them a pleafant and healthful exercife.

RECREATION LXII.

The uninvertible carriage.

HE body of this carriage must consist of a regular hollow globe, as A B (Plate X. Fig. 2.) at the bottom of which is to be an immoveable weight, and which must be proportioned to the number of persons, or the load the machine is intended to carry. Round the globe must go two horizontal iron circles D, E, and two others F, G, that are perpendicular to the former. All these circles must be made exactly to fit the globe, that it may move freely in every direction. The two horizontal circles are to be joined on each fide by a perpendicular bar, one of which is expressed in the figure by H I. All these irons should be lined with leather, to prevent unnecessary friction. The body of the carriage may be either of leather or hard wood, but the latter will be most elegible, as least liable to wear. The wheel

on each fide is to be fastened to the perpendicular bar by means of a handle K, that keeps it steady.

Now the body of this machine moveing freely in the iron circles, every way, the center of gravity will always lie at C; therefore in whatever position the wheels are, or even if they overturn, the body of the carriage will constantly remain in the same perpendicular direction.

At L is placed a pin, round which is a hollow moveable cylinder: this pin moves up and down in the groove M N, that it may not impede the perpendicular motion of the circles, at the fame time that it prevents the body of the machine from turning round in a horizontal direction. O, is one of the windows, P the door, and Q R the shafts to this machine.

When a carriage of this fort is intended for a fingle person, or a light weight,

manner as the rolling lamp or the fea compass, which will make its horizontal motion still more regular: and when it is designed to carry several persons, by adding another perpendicular bar, on each side, between the two horizontal circles, it may be placed on four wheels. The body of this machine should be frequently oiled or greased, not only to prevent any disagreeable noise that may arise from its rubbing against the circles, but to prevent unnecessary wear in the several parts.

This carriage is not intended for smooth roads, or a regular pavement; there, certainly, those of the common construction are much preferable; nor should a carriage totally free from irregular motion be sought after by those who are in perfect health: but there are many persons, subject to different disorders, who, by being obliged to travel over rough roads in the common carriages, suffer tortures of which the

PLATE.X Vol. I. 1. 200. G Fig. 1.p 202.



the healthful have no idea, to all these, therefore, and to every one who is forced to travel through dangerous roads, a carriage of this fort must doubtless be highly desirable.

As this design may appear to some perfons, on a superficial view, impracticable, we shall here insert an account of a similar carriage, which we have taken from the first volume of the Abridgement of the Philosophical Transactions, by Lowthorp, P. 592. There is not, however, any defcription of the manner in which that machine was constructed. The account is as follows: "A new fort of calesh described "by Sir R. B. This calesh goes on two "wheels; carries one person: is light " enough. Though it hangs not on braces " yet it is easier than the common coach. " A common coach will overturn if one " wheel go on a superficies a foot and a " half higher than the other, but this " will admit of the difference of three " foot

" foot and one third in height of the fu-" perficies, without danger of overturn-"ing. We chose all the irregular banks, "and fides of ditches, to run over, and I "have this day feen it, at five feveral "times, turn over and over, and the horse "not at all disordered. If the horse " should be in the least unruly, with the "help of one pin, you difengage him "from the calesh without any incon-" venience (a contrivance of this fort may " be easily added to the foregoing design.) "I myfelf have been once overturned, "and knew it not till I lookt up, and " faw the wheel flat over my head: and " if a man went with his eyes shut, he "would imagine himself in the most " fmooth way, though at the fame time "there be three foot difference in the " height of the ground of each wheel."

RECREATION, LXIII.

The columnar dial.

PLATE XI. Fig. 1. reprefents a column or obelisk AB, whose shaft GH is fluted, and divided by horizontal lines, that appear as joints, and ferve to mark the hours: the infide of this column is hollow, and is reprefented by Fig. 2: in the bafe is placed the hollow cylinder A, constructed exactly in the same manner with that of the 53d Recreation of this volume, but here it is kept in motion by the weight B, fastened to a string that goes over the pulley C, and to this string is likewife fastened the index H, that, as the weight defcends, points to the hours marked on the outfide of the column, as is expressed in Fig. 1, at H. The axis of the cylinder comes through the front of the column, and to the end of it is fixed an index that points to the minutes of each hour, mark-Vol. I. P

ed on a circle in the front of the base, as in Fig. 1. at B.

The striking part of this dial is contained in the capital of the column, (see Fig. 2.) where DE is an axis, on which are placed the two brass wheels F and G, that are of an equal diameter. On the circumference of the wheel G are six teeth, placed at equal distances from each other; these teeth are taken by the detent or lever IKL. The wheel F is likewise divided into six equal parts, in each of which is placed a different number of teeth from one to six. The short end of the detent or lever MNO takes the teeth of this wheel, and to the other end of it is sixed the hammer P, that strikes the bell Q.

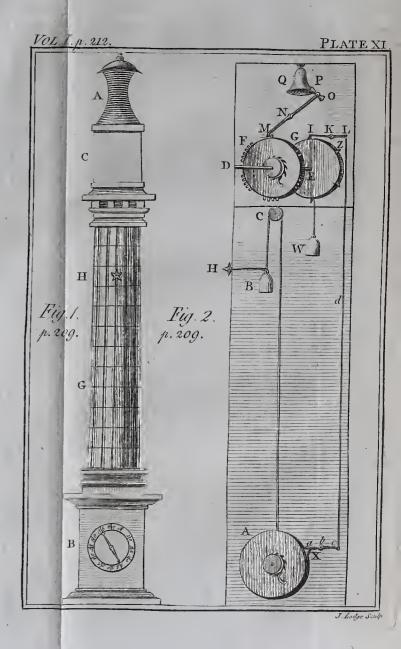
The wheel A making a complete revolution every hour, when it comes to X, its tooth raifes the end a of the lever a, b, c, confequently depresses the opposite end c, which by means of the string cd, raises

the end I of the lever IKL, and the wheel G is turned by the weight W from G to Z, but can go no farther; for the end I, of that lever, being heavier than the other end, descends again immediately after it has quitted the tooth. Now the wheel F being of the fame dimension as G, and fixed on the same axis, must necessarily move the fame space, in order to which it must push up the end of the lever MNO, that presses against one of its teeth, and that end descending again immediately, being heavier than the other, the hammer O will strike the bell; it will, in like manner, be forced over and fall between each tooth, till it come to the end of the divifion, and confequently give as many strokes on the bell as there are teeth in that divifion. As the end NO of the lever MNO is three times as long as MN, while the short end is pushed over one of the teeth, the other will be pushed three times as far from the bell.

Due care must be had in adjusting the weight to the effect it is to produce: for if it be too light, it will not overcome the friction of the lever with the teeth; and if it be too heavy, the wheel will move with too great velocity, and not give the lever sufficient time to fall in between the teeth. To the axis of each of the wheels A and F is fixed a racket-wheel and a ketch, by which they were wound up. The time of this dial's going may be considerably increased by adding one or more pullies to those at C and W.

It is evident from the construction of this dial that it strikes from one to six only: it may, however, be made to strike all the twelve hours, but then the number of teeth on the wheel F must be increased from 21 to 78, and consequently the wheels must be larger or the teeth smaller, either of which would be inconvenient; and as we have observed elsewhere, simplicity is a capital excellence in

the





the construction of every machine. It would certainly be more eligible for clocks in general to found no more hours than 6, as they would be less complex in their construction, the hours would be more readily told and less liable to be mistook; nor could it be attended with any inconvenience, as it is impossible for any one, to whom time is of the least importance, not to distinguish morning, noon, and night from each other.

A clock of this fort may be confiructed at a small expence and will make an elegant piece of furniture; or if elegance be not regarded, the machinery may be placed in the corner of a room, with a plain board before, and it will answer the intention, equally well. It is easy to conceive, that with a small alteration this machine may serve as a reveilleur or alarum.

RECREATION LXIV.

An air chronometer.

PROVIDE a glass tube (Plate XII. Fig. 1.) of about an inch diameter, and three or four feet long: the diameter of the inside of this tube must be precisely equal in every part: at the bottom is to be a small hole, that is closely covered with a valve. In the tube place a piston E, (Fig. 2.) which is made to fit it exactly, and must be oiled, that it may move in the tube with the greatest freedom: in this piston there is a cock, that shuts quite close, and from the top of it there goes a cord F, that passes through the handle G.

Now the cock of the piston being closed, it is to be let down to the bottom of the tube, and being then drawn up to the top, the air will rush in by the valve

at the bottom of the tube, and support the piston. You are then to turn the cock, so as to make a very small vent, and the air passing slowly through that vent, the piston will gradually descend and show the hour, either by lines cut in the tube with a diamond, or marked with paint, or by small slips of paper pasted on the glass. If this chronometer should go too fast or slow, it may be easily regulated by altering the position of the cock in the piston, as it is on that the whole depends.

If, instead of marking the tube, you would have the time shown by a dial, it may be easily effected by placing an axis, to which the hand of the dial is fixed, directly over the tube, and winding the string, to which the piston is joined, round that axis: for then as the piston descends the axis will gradually turn the hand, and show the hour: but you are

to observe, that as the descent of the piston is not constantly regular, occasioned by the decrease of resistance from the quantity of subjacent air as the piston descends, the axis, therefore must not be a regular cylinder, but conical, like the susee of a watch, as in Fig. 3. by which means the motion of the hand of the dial will be constantly uniform.

RECREATION LXV.

The lamp chronometer.

PLATE XII. Fig. 4. represents a chamber-lamp A, confifling of a cylindrical veffel about three inches high and one inch diameter, placed in the stand B. The infide of this veffel must be every where exactly of the fame diameter. To the stand B is fixed the handle C, which fupports the frame DEFG, about twelve inches high and four inches wide. This frame is to be covered with oiled paper, and divided into twelve equal parts, by horizontal lines; at the end of which are wrote the numbers for the hours, from I to 12, and between the horizontal lines are diagonals, that are divided into halves, quarters, &c. On the handle B, and close to the glass, is fixed the style or gnomon H.

Now as the distance of the style from the flame of the lamp is only half an inch, if the distance of the frame from the style be fix inches, then while the float that contains the light defcends, by the decrease of the oil, one inch, the shadow of the style on the frame will ascend twelve inches, that is, its whole length, and show by its progression, the regular increase of the hours, with their several divisions.

It is quite necessary that the oil used in this lamp be always of the fame fort, and quite pure, and that the wick also be constantly of the same size and substance, as it is on these circumstances and the uniform figure of the veffel, that the regular progress of the shadow depends.

To make this machine ornamental as well as useful, there may be drawn in the middle of the frame, yet fo as to leave the divisions of the hours quite visible, the

figures

figures of trees, flowers, animals, or whatever elfe the owner's imagination shall suggest; and if they be properly painted, in lively colours, they will have a very pleasing effect.

RECREATION LXVI.

The nocturnal dial.

HE two wheels A and B (Plate XII. Fig. 5.) are of the same diameter, and have each fifty-four teeth: their axis are parallel, but have no connection with each other. The pinion C and the wheel D have each fix teeth, and the wheel E eighteen teeth; the two last wheels, D and E, are placed on the fame axis: all thefe wheels must be of brass or copper, and as light as possible. Near the circumference of the wheel A are the figures for the hours and their divisions, which are cut through the plate, and covered with oiled paper.

paper. On the wheel B, at F, is fixed a lamp, the oil of which must be of the purest fort, and the wick constantly of the same size and matter; and round the axis of this wheel is wound a rope, to which hangs the weight G.

Now the quantity of oil in the lamp is fo adjusted, as to exactly counterbalance the weight G; but as the oil is continually decreasing, the weight must descend, though very gradually, and confequently turn the wheel B, and that must turn the pinion C and wheel D, which being fixed on the fame axis as E, turns that alfo, and confequently the wheel A. But as each of the great wheels A and B have fifty-four teeth, the pinion C and wheel D only fix teeth, and the wheel E eighteen teeth, it necessarily follows, that while the wheel B moves from F to H, that is, onethird of its circumference, the wheel A must make a complete revolution; and as fome

fome parts of its circumference will be continually opposite the lamp, the number of the hour will be always visible.

A hollow cone or funnel, as Fig. 6, is to be placed to that fide of the lamp oppofite the wheel A, the fmall end of this cone should be square, and which will confine the light of the lamp to a determinate part of the wheel A: if a moveable lens be adjusted to this small end, the quantity of light may be extended or contracted at pleasure.

This dial may be made to found the hours, by adding the apparatus described in the 63d Recreation, and fixing a tooth on the rini of the wheel A, against each hour, which will take the end of the lower lever, in the striking part of that machine, and it may like that ferve as an alarum.

To those who are troubled with an infomny, or inability to fleep, whether from constitution or disease, a dial of this fort will prove an agreeable companion, as it will continually show how the tiresome hours wear away; and to make it more amufing, over each hour fome motto may be cut out; for if the diameter of the wheel be one foot, its circumference will be fomething more than three feet, and confequently there will be a space of three inches to every hour. In the twelve compartments under the hours there may be likewife figures of hiftory, either religious or profane; or emblems of devotion, love, morality, or whatever elfe the temper and disposition of the owner may require; and if these figures be covered with transparent paper, properly coloured, this machine, at the fame time that it answers the common purposes of a dial and lamp, will afford a pleafing reprefentation; and as the wheels are in continual motion, and the

PLATE XII. Fig. 2. pv. 214. Fig. 4.p.217. Fig. 5. p.219. В



the light confined to a certain space, one that is continually varying.

We might here give a much greater variety of mechanical constructions, but we choose to confine ourselves to such as are most remarkable, and which, when duly confidered, will be quite fufficient to exemplify the foregoing aphorisms. They who are defirous of more variety, will readily find a great number of experiments that are conftantly repeated by every writer on mechanics.



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By adding as much to the amount of the figures that compose the number, as will make it divisible by nine.

RECREATION II. p. 23

A person having an even number of counters in one hand and an odd number in the other, to tell in which hand the odd or even number is.

By directing him to multiply the number in one hand by an odd number, and that in the other by an even number. and to tell you whether the amount of the two products be even or odd.

RECREATION III. p. 24

A person making choice of several numbers, another is to name him the number by which the sum of those numbers is divisible.

By putting a parcel of tickets, marked with numbers divifible by 3, into one divifion of a bag, and into another divifion tickets marked with the number 3 only, and letting two persons draw one from each division.

RECREATION IV. p. 25

To find the difference between two numbers, the greatest of which is unknown.

By fubtracting the least number from an equal number of nines, and directing another person to add to, and subtract from, the amount, in a determinate manner.

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RECREATION XI. p. 37

- Three dice being thrown on a table, to tell the number of each die, and the order in which they stand.
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- To tell the number a person has fixed on, without asking him any question.
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This number, which is 120, found by the foregoing table.

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RECREATION XXVII. p. 70

The ten duplicates.

Twenty cards being laid in pairs, and in four rows, feveral perfons are to look at different pairs, and tell you in which rows they are, when you tell them, by the aid of four Latin words, which cards they looked at.

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RECREATION XXVIII. p. 72

To name the number of cards that a person Shall take out of the pack.

This is done by previoufly disposing the cards in a certain order, and by an English verse to aid the memory.

RECREATION XXIX. p. 74

A century of different names being wrote on the cards, to tell the particular name that any person has thought on.

A hundred names are wrote on 10 cards, and the last name of each card begins with one of the letters of a word that has ten letters; and on ten other cards, the fame hundred names are wrote, in different dispositions. A person is to draw a card from the first ten, and after fixing on a name, give it you VOL. I. R again

again you then show him the other ten cards, and when he tells you the card that has the name, you tell him, by means of the last name on the card he drew, which it is. This recreation may be performed with twenty cards, instead of ten; and questions and answers may be used instead of names. 78

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The cards are here to be disposed after the same method as in the last recreation—the experiment is to fail at first, that it may appear the more extraordinary after the second shuffle.

RECREATION XXXII. p. 91

Several letters being wrote promiscuously upon 32 cards, after they have been once shuffled, to find on a part of them a question; and then shuffling the remainder a second time, to shew the answer.

The letters of the question and answer, which are 32, are to be wrote on the cards; the letters of the answer, which are ten, are to be wrote on a paper, and the numbers from 1 to to 10 assisted to them. They are then to be ranged by the second column of the table for ten numbers, and the whole thirty-two cards

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RECREATION XXXIII. p. 94

To write 32 letters on so many cards, then shuffle and deal them by twos to two persons in such manner, that the cards of one shall contain a question, and those of the other, the answer.

The numbers from 1 to 32 are to be wrote over the letters of the question and answer; they are then to be ranged according to the first column of the table for thirty-two numbers, shuffled and dealt.

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be found on thirty-two cards that are dealt to five perfons—the numbers from I to 32 are to be wrote over the letters of those words in a determinate order: the cards are then to be ranged according to the first column for thirty-two numbers. The five beatitudes being wrote, each of them on sour cards, each person is to draw one from one of the sours, and when the other cards are dealt, one by one, each person will have the same word on the cards dealt him as on that he drew.

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RECREATION XXXVI. p. 100

The cards at piquet being all mixed together, to divide the pack into two unequal parts, and name the number of points contained in each part.

The cards are to be disposed by the table for thrty-two numbers; they are then to to be shuffled, according to order and cut at a wide card, when each parcel will have a determinate number.

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The inconceivable repique.

This recreation is to be performed with the cards ranged in the order described R 4 in

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RECREATION XLV. p. 135

To tell the amount of the numbers of two cards that a person has drawn from a common pack of cards.

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by a fmall hole, from one partition to the other, causes the cylinder to defcend flowly and show the hour, by the ends of the axis pointing to a table of numbers on the wainscot.

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RECREATION LXIII. p. 209.

The columnar dial.

The case of this dial is a hollow column, in the base of which is the wheel that guides the hour and minute hands; and in the capital is the machinery that strikes the hours. On the shaft of the column the hours are marked by horizontal lines, to which an index points as it descends from the top of the shaft to the bottom; and on the base is a circle of minutes, marked by a hand sixed on the end of the wheel within.

RECREATION LXIV. p. 214

An air chronometer.

This chronometer confifts of a glass tube, wherein a piston is placed, that has a cock by which the subjacent air is suffered

fered to pass very flowly: as this piston descends it shows the hours, by divisions marked on the tube—a dial may be added to this chronometer, the hand of which may be moved by the string that is joined to the piston.

RECREATION LXV. p. 217.

The lamp chronometer.

The shadow of a style, placed before a lamp is thrown upon a frame covered with oiled paper, on which the hours and their divisions are marked. This instrument may be made ornamental as well as useful.

RECREATION LXVI. p. 219.

The nocturnal dial.

This dial confifts of two large and three finall wheels, a weight, a lamp, and a hollow

hollow cone. Through one of the large wheels, which is placed in the front of the machine, the figures for the hours are cut, on each of which the light of the lamp is directed to fall, by the hollow cone, in a regular progression—this dial may be made to found the hours, or serve as an alarm, p. 221.—method of making this machine exhibit a pleasing representation, p. 222.

THE END OF THE FIRST VOLUME.





